

Mathematics A

General Certificate of Secondary Education

Unit **A503/02**: Mathematics C (Higher Tier)

Mark Scheme for June 2012

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, OCR Nationals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

© OCR 2012

Any enquiries about publications should be addressed to:

OCR Publications
PO Box 5050
Annesley
NOTTINGHAM
NG15 0DL

Telephone: 0870 770 6622
Facsimile: 01223 552610
E-mail: publications@ocr.org.uk

Annotations used in the detailed Mark Scheme.

Annotation	Meaning
✓	Correct
✗	Incorrect
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working (after correct answer obtained), provided method has been completed
M0	Method mark awarded 0
M1	Method mark awarded 1
M2	Method mark awarded 2
A1	Accuracy mark awarded 1
B1	Independent mark awarded 1
B2	Independent mark awarded 2
MR	Misread
SC	Special case
^	Omission sign

These should be used whenever appropriate during your marking.

The **M**, **A**, **B** etc annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks.

It is vital that you annotate these scripts to show how the marks have been awarded.

It is not mandatory to use annotations for any other marking, though you may wish to use them in some circumstances.

Subject-Specific Marking Instructions

- 1 **M** marks are for using a correct method and are not lost for purely numerical errors.
A marks are for an accurate answer and depend on preceding **M** (method) marks. Therefore **M0 A1** cannot be awarded.
B marks are independent of **M** (method) marks and are awarded for a correct final answer or a correct intermediate stage.
SC marks are for special cases that are worthy of some credit.
- 2 Unless the answer and marks columns of the mark scheme specify **M** and **A** marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working **full marks** should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.

- 3 Where follow through (**FT**) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word *their* for clarity, eg FT $180 \times (\textit{their}'37' + 16)$, or FT $300 - \sqrt{(\textit{their}'5^2 + 7^2)}$. Answers to part questions which are being followed through are indicated by eg FT $3 \times \textit{their}(a)$.

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.

- 4 Where dependent (**dep**) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
- 5 The following abbreviations are commonly found in GCSE Mathematics mark schemes.
- **figs 237**, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point eg 237000, 2.37, 2.370, 0.00237 would be acceptable but 23070 or 2374 would not.
 - **isw** means **ignore subsequent working** (after correct answer obtained).
 - **nfw** means **not from wrong working**.
 - **oe** means **or equivalent**.
 - **rot** means **rounded or truncated**.
 - **seen** means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
 - **soi** means **seen or implied**.

- 6 Make no deductions for wrong work after an acceptable answer unless the mark scheme says otherwise, indicated for example by the instruction 'mark final answer'.
- 7 As a general principle, if two or more methods are offered, mark only the method that leads to the answer on the answer line. If two (or more) answers are offered, mark the poorer (poorest).
- 8 When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for **A** and **B** marks. Deduct 1 mark from any **A** or **B** marks earned and record this by using the MR annotation. **M** marks are not deducted for misreads.
- 9 Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75, which is seen in the working. The candidate then rounds or truncates this to 15.8, 15 or 16 on the answer line. Allow full marks for the 15.75.
- 10 If the correct answer is seen in the body of working
 - i. and the answer given in the answer space is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation ✓ next to the correct answer.
 - ii. but the answer space is blank, allow full marks. Place the annotation ✓ next to the correct answer.
 - iii. but a completely different answer is seen in the answer space, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation ✗ next to the wrong answer.
- 11 Ranges of answers given in the mark scheme are always inclusive.
- 12 For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
- 13 Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

Question			Answer	Marks	Part Marks and Guidance	
	(c)		UB = 75.5 LB = 74.5	1 1	Condone 75.5[0] or 75.49[9..] Condone 74.5[0] After 0 scored allow: SC1 for one correct value in wrong position	
3*			Shows fully correct calculation of both CI (4000×1.05^3 oe and 4630.5[0] or 630.5[0]) and SI (4000×1.15 oe and 4600 or 600) and that answer is £30.5 <u>0</u> . Well laid out answer with <u>correct and clear labelling</u> throughout.	5	<u>No misread allowed</u> other than 400 or 40000 used consistently	'Labelling' means identifying work as CI or SI and any other explanation. Accept 200, 210, 220.5[0] seen for 630.5[0] and 200, 200, 200 seen for 600
			Correct answers of (4630.5[0] or 630.5[0]) and (4600 or 600) and that answer is £30.5[0]. There may be little working shown and no/incorrect labelling.	4-3	<u>For lower mark</u> – Finds 4630.5[0] or 630.5[0] or (uses 4000×1.05^3 oe and 4000×1.15 oe). Any working is clear and well presented. Labelling may not be correct.	
			Finds 4600 or 600 or uses 4000×1.05^3 oe. Any working for that value is clear and well presented. Labelling may not be correct.	2-1	<u>For lower mark</u> - Finds 4200 or 200 or uses 4000×1.15 oe. Little structure to solution. Other work and labelling may not be correct.	
			No correct work or no relevant comment.	0		
4	(a)	(i)	0.3 oe nfw	2	M1 for $1 - (0.2 + 0.35 + 0.15)$ soi by answer of 0.48 <i>In this question – 1 once for poor notation in answers eg $\frac{0.3}{1}$ or 0.3 : 1 etc</i>	
		(ii)	0.55 oe	2	M1 for $0.2 + 0.35$ soi by answer of 0.37	

Question		Answer	Marks	Part Marks and Guidance	
	(b)	0.0225 oe	2	M1 for 0.15×0.15 oe	
	(c)	40	3	M2 for $8 \div 0.2$ oe or for <u>two</u> of 6 [red], 14 [blue], 12 [green] soi Or M1 for $8 = 0.2$, so $4 = 0.1$ oe soi or for <u>one</u> of 6[red], 14 [blue], 12 [green] soi	eg $16 = 0.4$
5	(a)	$21x + 18$ final answer	2	B1 for $21x$ or $[+]18$ seen	
	(b)	$10y - 24$ or $2(5y - 12)$ final answer	3	B1 for $6y - 30$ soi B1 for $6 + 4y$ soi After 0 scored allow: SC1 for $8y$ seen in answer	
6		Correctly evaluates one value from 2 to 3 inclusive Correctly evaluates one more value between 2 and 3 exclusive Correctly evaluates 2.7 to 2.732 and 2.7321 to 2.8 Answer 2.7 with justification	1 1 1 1	<i>Ignore incorrect trials</i> <i>Correct trials for 2.7 and 2.8 only or 2.7 and 2.75 only or 2.7 and 2.74 only implies the first 3 marks</i> Final mark dependent on 3 scored. Indicating outcome for 2.7 is closer to 4 or evaluating a value between 2.71 and 2.75 inclusive	<i>Their values rot to at least 1dp</i> 2 -4 2.1 -3.339 2.2 -2.552 2.3 -1.633 2.4 -0.576 2.5 0.625 2.6 1.976 2.7 3.483 2.71 3.6425 2.8 5.152 2.72 3.8036 2.9 6.989 2.73 3.9664 3 9 2.74 4.1308 2.75 4.2969
7	(a)	Large number of observations oe	1	Ignore extra statements	

Question		Answer	Marks	Part Marks and Guidance	
	(b)	$\frac{\text{Their}(\text{total of } 275, 255 \text{ and } 241)}{\text{Their}(\text{total of all 6 values})}$ $\frac{771}{1310} \text{ isw}$ <p>Or 0.58 to 0.59 or 58% to 59% Or 0.6 or 60%</p>	M2 A1	<p>For M2, allow rounded or truncated values B1 for 771 <u>or</u> 1310 seen</p> <p>Dependent on M2 scored</p>	<p>Also allow</p> <p>M2 for $\frac{275}{449}$ and $\frac{255}{450}$ and $\frac{241}{411}$ [0.61..., 0.56 to 0.57, 0.58 to 0.59 oe] Or M1 for $\frac{275}{449}$ or $\frac{255}{450}$ or $\frac{241}{411}$ oe</p> <p>OR</p> <p>M2 for $\frac{257}{436 \text{ to } 437}$ oe Or M1 for $(275 + 255 + 241) \div 3$ soi by 257 or for $(449 + 450 + 411) \div 3$ soi by 436 to 437</p>
8	(a)	(i)	(0, 5, 3)	1	
		(ii)	(6, 5, 0)	1	
		(iii)	(3, 0, 1.5)	1	
	(b)		9	2	M1 for $6 \times 3 \div 2$ oe
	(c)		8.36 to 8.4 or $\sqrt{70}$ final answer	3	<p>M2 for $6^2 + 5^2 + 3^2$ oe soi by 70 Or M1 for $(6^2 + 5^2)$ <u>or</u> $(6^2 + 3^2)$ <u>or</u> $(5^2 + 3^2)$ soi</p> <p>May be in two steps for M2</p>
9	(a)		186 000	1	
	(b)		$4.5[0..] \times 10^{13}$	2	<p>M1 for correct substitution of all values into formula or for answer figs 45</p> <p>For M1, condone any errors in conversion to ordinary numbers</p>

Question		Answer	Marks	Part Marks and Guidance	
	(c)	$c = \sqrt{\frac{E}{m}}$ or $c = \frac{\sqrt{E}}{\sqrt{m}}$ or $c = \sqrt{E \div m}$	2	B1 for correct form but with 'c =' omitted or for $c^2 = \frac{E}{m}$ Or SC1 for $c = \frac{\sqrt{E}}{m}$	
10	(a)	Splitting into rectangles and correctly finding the areas in terms of x	M2	M1 for splitting into rectangles and correctly trying to find area of one in terms of x	Eg for M2 $x \times x + 2x \times 3$ $x \times x + x \times 3 + x \times 3$ $x \times (x + 3) + x \times 3$ $2x \times (x + 3) - x \times x$ Etc
	(b)	7, 55	1, 1		
	(c)	5 or 6 points correctly plotted <u>Curve</u> joining 5 or 6 points	1FT 1FT	Within half small square of <i>their</i> 'correct' position Within half small square of <i>their</i> points	
	(d)	3.5 to 3.7 inclusive	1	Independent	
11	(a)	$(x - 5)(x - 2)$ 5 and 2	M2 B1	M1 for $(x + a)(x + b)$ where $a + b = -7$ or $ab = +10$	Final mark independent of method
	(b)	Substitute for y or equalise coefficients Obtain <u>any</u> correct equation in x (or y) $x = 3$ $y = -2$	M1 A1 B1 B1	Allow one error	Final 2 marks independent of method

Question		Answer	Marks	Part Marks and Guidance	
12	(a)	17.1	3	M2 for $\frac{19.5}{6.5} \times 5.7$ Or M1 for $\frac{19.5}{6.5}$ soi by 3	
	(b)	52	1		
	(c)	459 nfw	2	For 2 marks condone answer in range 452 to 460 nfw M1 for $51 \times (\text{their } 3)^2$	If using $A = \pi r^2$ must be full and complete method to score M1
13	(a)	3	1		
	(b)	Any three of 8, $28\sqrt{3}$, $10\sqrt{3}$, $35\sqrt{9}$ $113 + 38\sqrt{3}$ isw	M2 B1	M1 for any two of these	Accept 35×3 or 105 or $35\sqrt{3^2}$ for $35\sqrt{9}$ Final mark independent of method

Question	Answer	Marks	Part Marks and Guidance
14	$\frac{5}{12}$ oe isw nfw	5	<p>–1 for poor notation in answer</p> <p><u>EITHER</u> M2 for complete, correct tree diagram Or M1 for correct tree with no/wrong probs</p> <p><u>OR</u> M2 for identifying there are exactly 5 required pairs Some of these may be implied.....</p> <p>Or M1 for 3 of these</p> <p><u>AND</u> <u>EITHER</u> M2 for $\frac{1}{4} \times \frac{2}{3} + \frac{1}{4} \times \frac{2}{3} + \frac{1}{4} \times \frac{1}{3}$ oe Or M1 for $\frac{1}{4} \times \frac{1}{3}$ or $\frac{1}{4} \times \frac{2}{3}$ or $\frac{2}{4} \times \frac{2}{3}$ oe soi</p> <p><u>OR</u> M2 for identifying there are exactly 12 possible pairs. May be implied. Or M1 for 8 of these</p> <p>Must include probabilities for M2</p> <p>Eg (3, 5) (3, 5) (4, 4) (4, 5) (4, 5) Or in a 2-way table Eg (3, 5) oe and using probability 2/3 Or 5 in numerator of answer eg 5/20</p> <p>eg $\frac{1}{4} \times \frac{2}{3} + \frac{1}{4} \times \frac{2}{3} + \frac{1}{4} \times \frac{2}{3} + \frac{1}{4} \times \frac{2}{3} + \frac{1}{4} \times \frac{2}{3}$ oe Decimal equivalents rot to 2dp at least</p> <p>May be in a 2-way table More than 12 outcomes implies wrong work</p>

Question			Answer	Marks	Part Marks and Guidance
15			61.8 to 62 final answer	4	<p>Correct method with: Rads gives 81.8.. Grads gives 84.0...</p> <p>May be on diagram</p> <p><i>Their</i> 137 > 90</p> <p>ie <u>Any</u> equation with <u>two</u> sin terms and 25</p> <p>B1 for angles 137 <u>or</u> 16 seen AND M2 for $\frac{25}{\sin(\textit{their}16)} \times \sin(\textit{their}137)$</p> <p>Or M1 for any fully numerical attempt at sine rule</p>
16			$a = 2$ $a = 2k$ $b = 5$ or $b = 5k$ $c = -6$ $c = -6k$	1 1 2	<p>Any consistent $k \neq 0$</p> <p>M1 for $(\textit{their } b)^2 - 4 \times (\textit{their } a) \times c = 73$ oe</p> <p>Must be an equation</p>
17			550.18 to 551.09 final answer	5	<p><i>Final answer must be 2dp</i> <i>For answer 550 look back for 2dp value in range to score 5</i></p> <p>M2 for $(\pi \times 2.5 \times 3) \times 8.99$ Or M1 for $\pi \times 2.5 \times 3$ soi by 23.5 to 23.6 AND M2 for $(2 \times \pi \times 2.5 \times 2.4) \times 8.99$ Or M1 for $2 \times \pi \times 2.5 \times 2.4$ soi by 37.6 to 37.7</p> <p>Ignore any extra values calculated</p> <p>May find total area first before multiplying by 8.99 Multiplying by 8.99 may be implied</p>

Question		Answer	Marks	Part Marks and Guidance	
18		$\frac{4x-15}{(x-2)(x-3)}$ or $\frac{4x-15}{x^2-5x+6}$ final answer	3	SC2 for $\frac{2x^2-15}{(x-2)(x-3)}$ or $\frac{2x^2-15}{x^2-5x+6}$ or $\frac{-15}{(x-2)(x-3)}$ or $\frac{-15}{x^2-5x+6}$ OR M1 for common denominator $(x-2)(x-3)$ or x^2-5x+6 soi	Final answer Fractions may not be joined Condone any errors in multiplication. MUST be a quadratic
				And B1 for $x^2+5x-3x-15-x^2+2x$ oe soi	Condone one error May not be in a fraction

OCR (Oxford Cambridge and RSA Examinations)
1 Hills Road
Cambridge
CB1 2EU

OCR Customer Contact Centre

Education and Learning

Telephone: 01223 553998

Facsimile: 01223 552627

Email: general.qualifications@ocr.org.uk

www.ocr.org.uk

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored

Oxford Cambridge and RSA Examinations
is a Company Limited by Guarantee
Registered in England
Registered Office; 1 Hills Road, Cambridge, CB1 2EU
Registered Company Number: 3484466
OCR is an exempt Charity

OCR (Oxford Cambridge and RSA Examinations)
Head office
Telephone: 01223 552552
Facsimile: 01223 552553

© OCR 2012

