

GCE

Mathematics

Unit **4729**: Mechanics 2

Advanced GCE

Mark Scheme for June 2015

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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1. Annotations and abbreviations

| Annotation in scoris | Meaning |
|---|--|
| ✓ and ✖ | |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| ^ | Omission sign |
| MR | Misread |
| Highlighting | |
| | |
| Other abbreviations in mark scheme | Meaning |
| E1 | Mark for explaining |
| U1 | Mark for correct units |
| G1 | Mark for a correct feature on a graph |
| M1 dep* | Method mark dependent on a previous mark, indicated by * |
| cao | Correct answer only |
| oe | Or equivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |
| | |
| | |

2. Subject-specific Marking Instructions for GCE Mathematics (OCR) Mechanics strand

- a Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation ‘dep *’ is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)

We are usually quite flexible about the accuracy to which the final answer is expressed and we do not penalise over-specification.

When a value is given in the paper

Only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case.

When a value is not given in the paper

Accept any answer that agrees with the correct value to 3 s.f. +/-1 on the third significant figure.

ft should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination.

There is no penalty for using a wrong value for g . E marks will be lost except when results agree to the accuracy required in the question.

g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working.

'Fresh starts' will not affect an earlier decision about a misread.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

i If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j If in any case the scheme operates with considerable unfairness consult your Team Leader.

| Question | | Answer | Marks | Guidance |
|----------|------|--|---|--|
| 1 | (i) | $D = 480/v$ $480/v - 60 = 0$ $v = 8 \text{ m s}^{-1}$ | B1 M1 A1 [3] | Use of $D = P/v$ Use of N2L with 2 terms to find v |
| | (ii) | 600×14.2 $\frac{1}{2}(80)(9.4^2 - 8^2)$ $8520 = 974.4 + 60d$ $d = 126 \text{ m}$ | B1 B1ft M1 A1 [4] | WD by cyclist (8520 J) ft v from (i); KE gained (974.4 J); may be implied in energy equation Attempt at energy equation with all terms Exact 125.76 |
| 2 | | $T \cos \theta = 0.3g (= 2.94)$ $T \sin \theta = 0.3(0.343)(6^2) (= 3.7044)$ $T = 4.73 \text{ N}$ $\theta = 51.6^\circ$ | B1 M1 A1 M1 A1 A1 [6] | Resolve vertically or $T \sin a = 0.3g$; component of T required Attempt at use of N2L with $a = r\omega^2$ or $a = v^2/r$ Resolve horizontally or $T \cos a = 0.3(0.343)(6^2)$; component of T required Attempt to solve for T or θ ; component of T required in both equations SC if 38.4° then B1M1A1M1A1A0 5/6 Max |
| 3 | | $P/16$ or $P/25$ seen $P/16 - R = 1500(0.3875)$ or $P/25 - R = 1500(0.2)$ $P/16 - R = 1500(0.3875)$ and $P/25 - R = 1500(0.2)$ $P = 12\,500$ $R = 200$ | B1 M1 A1 M1 A1 A1 [6] | Use of Driving force = P/v Attempt to use N2L once, can be with D at this stage Both equations correct, may have consistent wrong sign with R Attempt to solve for P or R Allow 12.5 kW Allow if -ve, and justified why +ve (eg. comment on direction) |
| 4 | (i) | $2(8)\sin(\pi/2)/(3\pi/2)$ $(80 + 32\pi) x_G$ $= 80(2) + 32\pi(4 + cv(\text{CoM}))$ $x_G = 5(.00) \text{ cm}$ | B1 M1 A1 A1ft A1 [5] | CoM of semi-circle (3.395305...); $(32/3\pi)$ Table of values idea to get an equation/expression, using any fixed axis Relative to the axis they are using; ft their CoM (5.004444492 cm) |
| | (ii) | $4(20) = W(x_G \text{ from (i)} - 4)$ | M1 A1ft | Moments about E or A; allow wrong distance for either force ft on $cv(x_G)$; mg OK here; if $x_G < 4$ need $(4 - x_G)$ from (i) |

| Question | | Answer | Marks | Guidance |
|----------|-------|---|--|---|
| | | $4(20) = W(x_G \text{ from (i)})$ (Greatest) $W = 80 \text{ N}$ (Least) $W = 16 \text{ N}$ | A1ft A1 A1 [5] | ft on $cv(x_G)$; mg OK here 79.64601393 from exact x_G ; allow anything between 79.6 and 80 15.98579026 from exact x_G SC for masses found only, 4/5 for both 8.13 to 8.16 and 1.63 |
| 5 | (i) | $v^2 = 5^2 + 2g(1.6)$ $0.7 \times 7.507\dots (= 5.255\dots)$ $(0.7 \times cv(v))^2 = 2gh$ $h = 1.41 \text{ m}$ | B1 B1 M1 A1 [4] | Complete method to find $v (= 7.507\dots)$ $0.7 \times cv(v)$, but not $cv(v) = 5$; may be seen in (ii) Complete method to find h , with final speed 0; allow $cv(v) = 5$ for method Exact 1.409 |
| | (ii) | $0.2(7.507\dots)(0.7) - (-0.2)(7.507\dots)$ Impulse = 2.55 N s, upwards | M1 A1ft A1 [3] | Change in momentum found, with relevant velocities ie $cv(v)$ and $0.7 \times cv(v)$ but not $cv(v) = 5$ This may be negative; ft on their v found in (i) (2.5524...) Must have direction also. |
| | (iii) | $0.2(9.8)(1.6) + \frac{1}{2}(0.2)(5^2) - 0.2(9.8)(cv(h))$ OR $\frac{1}{2}(0.2)(7.507\dots)^2 - \frac{1}{2}(0.2)(0.7 \times 7.507\dots)^2$ Loss of energy = 2.87 J | M1 A1ft A1 [3] | Change in energy found, all energy terms needed and no extra terms This may be negative (2.87436 exact); art 2.87; allow -2.87 |
| 6 | (i) | $x = vt\cos\theta$ $y = vt\sin\theta - \frac{1}{2}gt^2$ $y = x \tan\theta - \frac{4.9x^2}{v^2 \cos^2\theta}$ | B1 B1 M1 A1 [4] | aef aef; may see this with t already eliminated Eliminate t www; AG |
| | (ii) | $-100 = 40\tan\theta - 4.9 \times 40^2 / (16^2 \times \cos^2\theta)$ $(30.625\tan^2\theta - 40\tan\theta - 69.375 = 0)$ | M1 A1 A1 | Attempt to substitute values into trajectory equation aef; obtain correct quadratic in $\tan\theta$, may be unsimplified |

| Question | | Answer | Marks | Guidance |
|----------|------|--|---|--|
| | | $(\tan\theta = 2.2937\dots \text{ or } -0.9876\dots)$ $\theta = 66.4$ $\theta = -44.6$ | M1 A1 A1 [6] | Attempt to solve quadratic in $\tan\theta$ Allow 44.6 below the horizontal |
| 7 | (i) | $2W(1\cos\theta) + W(2\cos\theta) = R_B(4\sin\theta)$ $R_A = 3W$ $\mu = 2/3$ | *M1 A1 A1 B1 dep*M1 A1 [6] | Moments about A, all terms needed and no extra; dimensionally correct; each term must include $\sin\theta$, or $\cos\theta$ or $\tan\theta$ May have Fr for R_B Use of $Fr = \mu R_A$ to get an equation in W (or R_A) only AG ; must come from exact θ |
| | OR | $W(2\cos\theta) + 2W(3\cos\theta) + Fr(4\sin\theta) = R_A(4\cos\theta)$ $R_A = 3W$ $\mu = 2/3$ | *M1 A1 A1 B1 dep*M1 A1 [6] | Moments about B, all terms needed and no extra; dimensionally correct; each term must include $\sin\theta$, or $\cos\theta$ or $\tan\theta$ Use of $Fr = \mu R_A$ to get an equation in W (or R_A) only AG ; must come from exact θ |
| | (ii) | $(W + aW)(2\cos\theta) = R_B(4\sin\theta)$ $R_A = 3W + aW$ $a \leq 3$ | *M1 A1 B1 dep*M1 A1 [5] | Moments about A, all terms needed and no extra; dimensionally correct; each term must include $\sin\theta$, or $\cos\theta$ or $\tan\theta$ May have Fr for R_B Resolve vertically $Fr \leq \mu R_A$ to get an inequality in W and a only; allow equality here Allow $a < 3$. If using equality, correct inequality need not be justified. |
| | OR | For first 2 marks $(W + aW)(2\cos\theta) + 2W(4\cos\theta) + Fr(4\sin\theta) = R_A(4\cos\theta)$ | *M1 A1 | Moments about B, all terms needed and no extra; dimensionally correct; each term must include $\sin\theta$, or $\cos\theta$ or $\tan\theta$ |
| 8 | (i) | $0.4v^2/0.6 = 6, v = 3$ | M1 A1 [2] | Attempt at use of N2L with $a = v^2/r$ or $a = r\omega^2$; allow verification. AG If +/-3 then -3 must be rejected for A1. |
| | (ii) | | *M1 | Attempt at use of conservation of linear momentum |

| Question | | Answer | Marks | Guidance |
|----------|--------------|---|--|--|
| | | $3(0.4) = 0.4v_A + 0.5v_B$ $v_B - v_A = 3(0.35)$ $v_A = 0.75 \text{ m s}^{-1}$ and $v_B = 1.8 \text{ m s}^{-1}$ | A1 *M1 A1 dep*M1 A1 [6] | Attempt at use of restitution equation, must be correct way round Must be consistent with the directions used for CoLM Solving simultaneous equations Both values positive as final answer. |
| | (iii) | $Y = 0.4g (= 3.92)$ $(4.9)^2 - (0.4g)^2 (= 2.94^2)$ $0.4(0.6)\omega^2 = cv(2.94)$ $\omega = 3.5$ | B1 B1 M1 A1 [4] | Resolve vertically Use of Pythagoras Resolve horizontally, cv(2.94) from a legitimate attempt at 2.94 Exact |
| | OR | $4.9\cos\theta = 0.4g$ $\cos\theta = 0.8$ or $\theta = 36.9$ $0.4(0.6)\omega^2 = 4.9\sin\theta$ $\omega = 3.5$ | B1 B1 M1 A1 [4] | Resolve vertically, θ angle with vertical Resolve horizontally, θ substituted and from a legitimate attempt Exact |
| | OR | $Y = 0.4g (= 3.92)$ $X = 0.4(0.6)\omega^2 (= 0.24\omega^2)$ $(0.4g)^2 + (0.4(0.6)\omega^2)^2 = 4.9^2$ $\omega = 3.5$ | B1 B1 M1 A1 [4] | Resolve vertically Resolve horizontally Attempt at use of Pythagoras, from a legitimate attempt at X Exact |

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