

# **GCE**

# **Mathematics (MEI)**

Unit 4754A: Applications of Advanced Mathematics: Paper A

Advanced GCE

Mark Scheme for June 2017

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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# **Annotations and abbreviations**

| Annotation in scoris               | Meaning  |
|------------------------------------|--|
| ✓ and X                            |  |
| BOD                                | Benefit of doubt   |
| FT                                 | Follow through   |
| ISW                                | Ignore subsequent working                                |
| M0 M1                              | Method mark awarded 0, 1                                 |
| A0 A1                              | Accuracy mark awarded 0, 1                               |
| B0 B1                              | Independent mark awarded 0, 1                            |
| SC                                 | Special case   |
| ^                                  | Omission sign  |
| MR                                 | Misread  |
| Highlighting                       |  |
|                                    |  |
| Other abbreviations in mark scheme | Meaning  |
| E1                                 | Mark for explaining                                      |
| U1                                 | Mark for correct units                                   |
| G1                                 | Mark for a correct feature on a graph                    |
| M1 dep*                            | Method mark dependent on a previous mark, indicated by * |
| cao                                | Correct answer only                                      |
| oe                                 | Or equivalent  |
| rot                                | Rounded or truncated                                     |
| soi                                | Seen or implied  |
| www                                | Without wrong working                                    |

# Subject-specific Marking Instructions for GCE Mathematics (MEI) Pure strand

a Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

c The following types of marks are available.

#### М

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

#### Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

#### В

Mark for a correct result or statement independent of Method marks.

#### Ε

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep \*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.
- g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

| ( | Questi | on | Answer   | Marks              | Guidance  |
|---|--------|----|--|--------------------|---|
| 1 | (i)    |    | $\frac{5-x}{(2-x)(1+x)} = \frac{A}{2-x} + \frac{B}{1+x}$ $\Rightarrow 5-x = A(1+x) + B(2-x)$ $x = 2 \Rightarrow 3 = 3A, A = 1$ | M1<br>A1           | Cover up, substitution or equating coefficients   |
|   |        |    | $x = -1 \Rightarrow 6 = 3B \Rightarrow B = 2$  | A1<br>[ <b>3</b> ] |   |
|   | (ii)   |    | $\frac{A}{2-x} = \frac{A}{2} (1 - \frac{1}{2}x)^{-1}$  | B1                 | Or equivalent   |
|   |        |    | $= \frac{A}{2}(1 + (-1)(-\frac{1}{2}x) + \frac{(-1)(-2)}{2!}(-\frac{1}{2}x)^2 + \dots)$  | M1                 | All three correct <b>unsimplified</b> binomial coefficients (not nCr) soi <b>for either expansion</b> i.e. 1, $-1$ and $\frac{(-1)(-2)}{2}$ . Or correct simplified coefficients seen |
|   |        |    | $= A \left( \frac{1}{2} + \frac{1}{4}x + \frac{1}{8}x^2 + \dots \right)$   | A1ft               | Ignore any subsequent incorrect terms – ft their A from (i) only  |
|   |        |    | $\frac{B}{1+x} = B(1+x)^{-1} = B(1-x+x^2+)$  | A1ft               | Ignore any subsequent incorrect terms – ft their <i>B</i> from (i) only   |
|   |        |    | $\frac{5-x}{(2-x)(1+x)} = \frac{5}{2} - \frac{7}{4}x + \frac{17}{8}x^2 + \dots$  | A1                 | www cao – ignore any higher order terms stated – isw after correct expansion seen   |
|   | (2)    |    | 1.22   | [5]                |   |
| 2 | (1)    |    | $x = -1 + 2\lambda$ , $y = -3\lambda$ , $z = 1 + \lambda$  | M1*                | Condone a single sign slip – maybe implied by later working   |
|   |        |    | $\Rightarrow 3(-1+2\lambda)+4(-3\lambda)-(1+\lambda)=17$   | M1dep*             | Substituting their <i>x</i> , <i>y</i> and <i>z</i> into the correct plane equation (condone a further single slip if intention clear)  |
|   |        |    | $\Rightarrow -7\lambda = 21, \ \lambda = -3$   | A1                 | www cao   |
|   |        |    | point of intersection is therefore (-7, 9, -2)   | A1                 | www cao – condone $x = -7$ , $y = 9$ , $z = -2$ – condone answer given as a column vector   |
|   |        |    |  | [4]                |   |
|   |        |    |  |                    |   |

| Question | Answer  | Marks | Guidance   |
|----------|---|-------|--|
| (ii)     | $\mathbf{u} = 3\mathbf{i} + 4\mathbf{j} - \mathbf{k},  \mathbf{v} = 2\mathbf{i} - 3\mathbf{j} + \mathbf{k}$                                     | B1    | Identifying and using vectors <b>u</b> and <b>v</b> and no other vectors   |
|          | $\cos \theta = \frac{3 \times 2 + 4 \times (-3) + (-1) \times 1}{\sqrt{26} \sqrt{14}}$  | M1    | Correct formula (including cosine), with correct substitution of their <b>u</b> and their <b>v</b> – with at least one vector correct. Condone either a single numerical slip <b>or</b> a single sign slip (but not one of each) if intention is clear. It must be clear where the slip comes from e.g. if the magnitude of one vector is stated incorrectly with no working then M0 |
|          | $\theta$ = 111.5°   | A1    | Allow 111 or 112 or 1.94 or 1.95 (must come from correct working) –  |
|          |   |       | may be implied by the correct answer of 68.5   |
|          | so acute angle between line and normal is 68.5°   | A1    | www cao (or 1.20 in radians) or better (68.47546, 1.195122) A0 if choice of answers  |
|          |   |       | If sine used then it must be a complete method for finding the correct   |
|          |   |       | angle - so for the M mark need to see  |
|          |   | [4]   | $\theta = \sin^{-1} \left( \frac{3 \times 2 + 4 \times (-3) + (-1) \times 1}{\sqrt{26} \sqrt{14}} \right) + 90^{\circ} \text{ (oe) if no attempt to add } 90 \text{ M0}$   |
| 3 (i)    | $T_4 < T_2$   | B1    | oe (e.g. $T_4$ is less than $T_2$ )  |
|          | The approximation is an over-estimate, as the trapezia are above the curve therefore the error becomes less when the number of strips increases | B1    | Must see mention of 'over-estimate' and 'above' and 'increasing strips'  |
|          | •   | [2]   |  |
| (ii)     | $0.5 \times 0.5$  | B1    | For using 0.25 oe  |
|          | $\{1.0655+2.8963+2(1.1695+1.4142+1.9282)\}$   | M1    | The M mark requires the correct {} bracket structure. It needs the   |
|          |   | A1    | first bracket to contain the first y value plus the last y value and the second bracket to be multiplied by 2 and to be the summation of the remaining y values with no additional values. Allow an error in one value <b>or</b> the omission of one value from the second bracket M0 if using x values. All values given to at least 3sf or exact                                   |
|          |   |       | The A mark is for the correct {} bracket with no errors (12.98 or  |
|          | $T_4 = 3.25$  | A1    | 13.0 implies M1A1) cao (3.25 with no working scores 0/4) – must be given to 2dp only (for reference correct answer is 3.2465079) SC: bracketing error 0.25×(1.0655+2.8963)+2(1.1695+)  |
|          |   | [4]   | scores B1M1A0A0 unless the final answer implies the correct calculation. An answer of 10.014 usually indicates this error  |

|   | Question | Answer  | Marks  | Guidance  |
|---|----------|---|--------|---|
|   | OR       | 0.5587+ 0.6459 + 0.8356+ 1.2061   |        | Separate trapezia<br>B1 – one area correct (implies 0.25)   |
|   |          |   |        | M1 – three correct (equivalent to one error)  |
|   |          |   |        | A1 – all four correct   |
|   |          |   |        | A1 – cao of 3.25  |
| 4 |          | $ \mathbf{v}  = \sqrt{a^2 + b^2 + 25} = \sqrt{27}$  | M1*    | Condone one error on either lhs or rhs (but not both)   |
|   |          | $\Rightarrow a^2 + b^2 = 2$   | A1     | oe - allow unsimplified but square roots must be removed  |
|   |          | a - 7b - 10 = 0   | B1     | cao (oe) – must include = 0 (if all terms collected on one side)  |
|   |          | $a = 7b + 10 \Rightarrow (7b + 10)^2 + b^2 = 2$   | M1dep* | Correct method for solving their simultaneous equations — which would result in a three-term quadratic equation (= $0$ maybe implied) in either $a$   |
|   |          |   |        | or $b$ – if correct the equation in $a$ is $49a^2 + (a-10)^2 = 98$  |
|   |          | $b = -\frac{7}{5}$  | A1     | www cao   |
|   |          | $a = \frac{1}{-}$   | A1     | www cao - award B1 for each correct answer if no working seen   |
|   |          | 5   | [6]    |   |
| 5 |          | $4\tan \theta \tan 2\theta = 1 \Rightarrow 4\tan \theta \cdot \frac{2\tan \theta}{1 - \tan^2 \theta} = 1$ | M1*    | Use of double angle formula for tan to get an equation in tan – allow one sign slip only  |
|   |          | $\Rightarrow 8\tan^2\theta = 1 - \tan^2\theta$  |        |   |
|   |          | $\Rightarrow \tan^2 \theta = 1/9$   | M1dep* | Re-arranges to $\tan^2 \theta = k$ where $k > 0$ or attempt to solve  |
|   |          |   |        | $a \tan^2 \theta - b = 0$ where $b/a > 0$   |
|   |          | $\tan \theta = 1/3 \text{ or } -1/3$  |        |   |
|   |          | $\theta = 18.43^{\circ} \text{ or } 161.57^{\circ}$   | A1     | One correct answer to at least 1dp  |
|   |          | $\theta = 18.43^{\circ} \text{ and } 161.57^{\circ}$  | A1     | Both answers correct to at least 1dp  |
|   |          |   | [4]    | SC A1A0 for answers which round to 0.322 <b>and</b> 2.82 (radians) Answers with no working can score B1 B1 (max 2/4) if correct Ignore additional solutions outside the range. If any additional solutions given inside the range of $0 < \theta < 180$ and full marks would have been awarded then remove last mark (so 3/4) |

|   | Question |    | Answer   | Marks     | Guidance   |
|---|----------|----|--|-----------|--|
| 6 | (i)      |    | $\frac{\mathrm{d}P}{\mathrm{d}t} = k\sqrt{P}$  | B1<br>[1] | oe – condone $dP = k\sqrt{P}dt$  |
|   | (ii)     |    | $P = (A + Bt)^2 \Rightarrow \frac{\mathrm{d}P}{\mathrm{d}t} = 2(A + Bt)B$  | M1        | Attempt at chain rule – allow this mark if $B$ absent or incorrect but must include $2(A+Bt)$ - if multiplied out condone one error in differentiation   |
|   |          |    | $\frac{\mathrm{d}P}{\mathrm{d}t} = 2B\sqrt{P}$   | A1        | oe - correctly showing that the rate of increase of $P$ is proportional to the square root of $P$  |
|   |          |    | k = 2B   | A1<br>[3] | Not for $B = \frac{k}{2}$  |
|   |          | OR | $\int \frac{\mathrm{d}P}{\sqrt{p}} = k \int \mathrm{d}t \Rightarrow 2\sqrt{P} = kt(+c)$ $P = \left(\frac{1}{2}kt + A\right)^2$ | M1        | Separates their variables correctly and attempt to integrate for their differential equation given in (i) – for an attempt powers must increase by 1 (oe) but not for $k$ – condone lack of + $c$                |
|   |          |    | $P = \left(\frac{1}{2}kt + A\right)^2$   | A1        | Correct integration - accept any (correct) constant for $A$ - coefficient of $t$ maybe implicit stated e.g. $P = (Ct + A)^2$ with $k = 2C$ seen  |
|   |          |    | k = 2B   | A1        | Not for $B = \dots$  |
| 7 | (i)      |    | $k = 2B$ $\int 4(y+3)  \mathrm{d} y = \int 9x  \mathrm{d} x$   | M1        | Separating variables – if no subsequent work then integral signs needed, but allow omission of dx and/or dy but must be correctly placed if present – allow errors in re-arranging but x and y on separate sides |
|   |          |    | $2y^2 + 12y = \dots$   | A1        | oe - Correct integration of y terms (or $2(y+3)^2$ oe)   |
|   |          |    | $\ldots = \frac{9}{2}x^2(+c)$  | A1        | oe - Correct integration of $x$ terms – condone omission of + $c$ for these two A marks  |
|   |          |    | when $x = 0$ , $y = 0$ , $\Rightarrow 0 = 0 + c$ , so $c = 0$  | B1        | cao (previous three marks must have been awarded) – need to show that $c=0$ . As a minimum $x=0$ , $y=0$ , $c=0$   |
|   |          |    | $\Rightarrow 4y^2 + 24y = 9x^2$  |           |  |
|   |          |    | $\Rightarrow 9x^2 - 4y^2 - 24y = 0$ *  | A1        | AG www (dependent on all previous marks in this part) – must show at least one step of intermediate working after integration – must have = 0  |
|   |          |    |  |           | SC: working backwards – B1 for $18x - 8y \frac{dy}{dx} - 24 \frac{dy}{dx} = 0$ and then B1 for   |
|   |          |    |  | [5]       | re-arranging correctly to $\frac{dy}{dx} = \frac{9x}{4(y+3)}$ (so max. 2/5)  |

| Question | Answer  | Marks     | Guidance  |
|----------|---|-----------|---|
| (ii)     | $V = \pi \int_0^2 x^2  \mathrm{d} y$  | M1        | M1 for $k(\pi) \int_0^2 x^2(dy)$ with correct limits and $k = 1$ or $\frac{1}{2}$ , allow correct limits seen or implied later. If formula not stated then must substitute for their $x^2$ to imply this formula – condone lack of $\pi$ for the M mark and dy throughout (condone incorrect use of dx too) |
|          | $= \pi \int_0^2 \frac{4}{9} (y^2 + 6y)  \mathrm{d} y$   | A1        | Correct (or with a factor of ½) – limits may be seen or implied through later working   |
|          | $= \pi \int_0^2 \frac{4}{9} (y^2 + 6y)  dy$ $\frac{4}{9} \left( \frac{y^3}{3} + 3y^2 \right)$ $= \frac{176}{27} \pi \text{ or } 6\frac{14}{27} \pi$ | B1        | or $\frac{2}{9} \left( \frac{y^3}{3} + 3y^2 \right)$ (but only if $k = \frac{1}{2}$ )   |
|          | $= \frac{176}{27} \pi \text{ or } 6\frac{14}{27} \pi$   | A1<br>[4] | Exact (oe) – mark final answer (so no isw if correct answer is e.g. halved) but if exact value seen and is then followed by 20.4785 then isw  |
|          |   |           |   |
|          |   |           |   |
|          |   |           |   |
|          |   |           |   |

| Quest | ion | Answer  | Marks | Guidance  |
|-------|-----|---|-------|---|
| (iii) | (A) | = $9(2 \tan \theta)^2 - 4(3(\sec \theta - 1))^2 - 24(3(\sec \theta - 1))$                 | M1    | Sub. for x and y – condone one slip e.g. using $3 \sec \theta - 1$  |
|       |     | $= 36 \tan^2 \theta - 36 \sec^2 \theta + 72 \sec \theta - 36 - 72 \sec \theta + 72$       | A1    | cao (multiplied out) – accept if = 0 and multiplied out correctly   |
|       |     | $= 36 \tan^2 \theta - 36 (1 + \tan^2 \theta) + 72 \sec \theta - 36 - 72 \sec \theta + 72$ | M1    | Use of correct formula $\sec^2 \theta = 1 + \tan^2 \theta$ (or $\sin^2 \theta + \cos^2 \theta = 1$ if converted to $\sin/\cos$ ) soi - maybe awarded before previous A mark – for those that set the lhs = 0 this mark can be awarded for a clear attempt to derive one of these identities   |
|       |     | =-36-36+72=0*   | A1    | AG www – all working must be explicitly shown including use of relevant Pythagorean identity. If candidates set their expression equal to zero then all four marks can be awarded provided all working is correct (so no dividing through by a constant before the expression has been put equal to zero) <b>and</b> a conclusion is required (so for those that derive a correct trig. identity then we must see a statement such as 'true' etc. accept as a minimum a tick. If following working from both sides of their equation $0 = 0$ seen then either a statement or re-stating the equation $9x^2 - 4y^2 - 24y = 0$ is required) – no $\theta$ missing in tan etc. |
| (iii) | (B) | $\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{18\tan\theta}{12\sec\theta}$                     | B1    | Maybe implied by later working  |
|       |     | $=\frac{18\frac{\sin\theta}{\cos\theta}}{12\frac{1}{\cos\theta}}$                         | M1    | Correct use of both $\tan \theta = \frac{\sin \theta}{\cos \theta}$ and $\sec \theta = \frac{1}{\cos \theta}$ give bod if stated somewhere in their solution  |
|       |     | $=\frac{3}{2}\sin\theta$  | A1    | $k = \frac{3}{2}$ oe - need not be explicitly stated so accept $\frac{3}{2}\sin\theta$  |
|       |     | when $x = 2$ , $\theta = \pi/4$   | B1    | Must be exact – condone $\theta = 45^{\circ}$ or $y = 3(\sqrt{2} - 1)$  |
|       |     | $\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{3}{2}\sin\frac{\pi}{4} = \frac{3}{2\sqrt{2}}$    | A1    |   |
|       |     |   | [9]   | correct final answer implies previous B mark  |

| Question | Answer  | Marks                | Guidance  |
|----------|---|----------------------|---|
| 8 (i)    | x = 1   | B1                   | Condone if derived from $\theta = \pi$  |
|          | $\theta = 0$  | B1                   | Must be explicitly stated   |
|          | $y = \cos 0 + 2\sin 0 = 1$ , (so B is (1, 1))   | B1 [3]               | www (not from $2\theta = 2\pi$ ) - condone $x = 1$ and $y = 1$  |
| (ii)     | $\cos\theta + 2\sin\theta = R(\cos\theta\cos\alpha + \sin\theta\sin\alpha)$   | - 1                  |   |
|          | $\Rightarrow R\cos\alpha = 1, R\sin\alpha = 2$  | M1 A1                | Correct pairs. Condone sign errors only for the M mark – allow use of $\theta$ for $\alpha$ only if recovered later by stating a value for $\tan \alpha$ or $\alpha$ not $\theta$   |
|          | $R^2 = 1^2 + 2^2 = 5 \Rightarrow R = \sqrt{5}$  | B1                   | Or 2.24 or better, not $\pm \sqrt{5}$ unless $+\sqrt{5}$ chosen   |
|          | $\tan \alpha = 2 \Rightarrow \alpha = 1.107$  | M1 A1                | For M1 ft their pairs (condone sign errors but division must be the correct way round).  A1 for 1.107 or better (accept 1.11), with no errors seen in method for angle – A0 if in degrees  SC: If candidates state that $\cos \alpha = 1$ , $\sin \alpha = 2 \Rightarrow \tan \alpha = 2$ this could score M0 A0 B1 M1 A1 (so max 3/5)  Note that candidates who state the correct values of $R$ and $\alpha$ with no |
|          |   | [5]                  | (wrong) working seen can score full marks   |
| (iii)    | At A, $\cos(\theta - \alpha) = 0$ , so $\theta - \alpha = \pi/2$ , $\theta = 2.678$<br>Or $\cos\theta + 2\sin\theta = 0 \Rightarrow 1 + 2\tan\theta = 0 \therefore \theta = -0.464$ | B1ft                 | $\theta = \frac{\pi}{2} + \text{their } \alpha \ (\theta = 2.677945) \text{ or } -0.4636476 \text{ from tan - allow}$   |
|          | x = 0.6, y = 0  | B1                   | in degrees ( $-26.56505$ ) www their $x$ value must be given exactly or correctly rounded to $0.6$ (condone trailing 0s) but do not accept $0.600087$ must also state $y = 0$   |
|          | At C, $cos(\theta - \alpha) = 1$ , so $\theta - \alpha = 0$ , $\theta = 1.107$  | B1ft                 | $\theta$ = their $\alpha$ from (ii) (allow $\theta$ = 2.03444) - allow in degrees (63.4349) or from $-\sin\theta + 2\cos\theta = 0$ (condone if stated as dy/dx)  |
|          | x = -0.6  | B1                   | www exact or correctly rounded to -0.6 (do not accept e.g0.5997 as their final answer)  |
|          | $y = \sqrt{5}$  | B1ft<br>[ <b>5</b> ] | Exact or 2.24 or better (2.2360679) or ft their <i>R</i>  |

| Questi | ion | Answer   | Marks     | Guidance   |
|--------|-----|--|-----------|--|
| (iv)   |     |  | M1*       | M1 for their $(dy/d\theta)$ / their $(dx/d\theta)$ in terms of $\theta$ with at least one                                  |
|        |     | $\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\mathrm{d}y/\mathrm{d}\theta}{\mathrm{d}x/\mathrm{d}\theta} = \frac{2\cos\theta - \sin\theta}{-2\sin2\theta}$ | A1        | term correct (soi) cao (oe) – allow unsimplified even if subsequently cancelled incorrectly i.e. can isw                   |
|        |     | when $\theta = 2.678$ , $\frac{dy}{dx} = -1.398$ or $\theta = -0.464$ , $\frac{dy}{dx} = 1.398$  | A1        | Allow $\pm 1.40$ or better ( $\pm 1.3975424$ )   |
|        |     | $\tan \frac{1}{2}\beta = 1.398$  | M1dep*    | $\tan\left(\frac{1}{2}\beta\right) = \pm \frac{dy}{dx}\Big _{\theta \text{ at A}}$ so this mark can be awarded for putting |
|        |     |  |           | $\tan\left(\frac{1}{2}\beta\right)$ equal to either +/- their numerical gradient at A but must be                          |
|        |     |  |           | using $\theta$ values and not x values   |
|        |     | angle between branches = 1.90 (radians)  | A1<br>[5] | 1.90 or better (1.8994312) – not in degrees  |

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