

Methods in Mathematics (Pilot)

General Certificate of Secondary Education

Unit **B392/02**: Higher Tier

Mark Scheme for January 2012

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Annotations

used in the detailed Mark Scheme.

Annotation	Meaning
✓	Correct
✘	Incorrect
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working (after correct answer obtained), provided method has been completed
M0	Method mark awarded 0
M1	Method mark awarded 1
M2	Method mark awarded 2
A1	Accuracy mark awarded 1
B1	Independent mark awarded 1
B2	Independent mark awarded 2
MR	Misread
SC	Special case
^	Omission sign

These should be used whenever appropriate during your marking.

The **M**, **A**, **B**, etc annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks.

It is vital that you annotate these scripts to show how the marks have been awarded.

It is not mandatory to use annotations for any other marking, though you may wish to use them in some circumstances.

M marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding **M** (method) marks. Therefore **M0 A1** cannot be awarded.

B marks are independent of **M** (method) marks and are awarded for a correct final answer or a correct intermediate stage.

SC marks are for special cases that are worthy of some credit.

Unless the answer and marks columns of the mark scheme specify **M** and **A** marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working **full marks** should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.

Where follow through (**FT**) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word *their* for clarity, eg FT $180 \times (\textit{their} '37' + 16)$, or FT $300 - \sqrt{(\textit{their} '5^2 + 7^2')}$. Answers to part questions which are being followed through are indicated by eg FT $3 \times \textit{their}$ (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.

Where dependent (**dep**) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.

The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- **cao** means **correct answer only**.
- **figs 237**, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point eg 237000, 2.37, 2.370, 0.00237 would be acceptable but 23070 or 2374 would not.
- **isw** means **ignore subsequent working** (after correct answer obtained).
- **nfww** means **not from wrong working**.
- **oe** means **or equivalent**.
- **rot** means **rounded or truncated**.
- **seen** means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- **soi** means **seen or implied**.

Make no deductions for wrong work after an acceptable answer unless the mark scheme says otherwise.

As a general principle, if two or more methods are offered, mark only the method that leads to the answer on the answer line. If two (or more) answers are offered, mark the poorer (poorest).

When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for **A** and **B** marks. Deduct 1 mark from any **A** or **B** marks earned and record this by using the **MR** annotation. **M** marks are not deducted for misreads.

Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75, which is seen in the working. The candidate then rounds or truncates this to 15.8, 15 or 16 on the answer line. Allow full marks for the 15.75.

If the correct answer is seen in the body and the answer given in the answer space is a clear transcription error allow full marks unless the mark scheme says 'mark final answer' or 'cao'. If the answer is missing, but the correct answer is seen in the body allow full marks. If the correct answer is seen in working but a completely different answer is seen in the answer space, then accuracy marks for the answer are lost. Method marks would still be awarded.

Ranges of answers given in the mark scheme are always inclusive.

For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.

Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

Question			Answer	Marks	Guidance	
1	(a)		3.24 isw	2	<p>M1 for 0.15×21.60 or eg using 10% and 5% with 10% = 2.16 or 1% = 0.216 then $\times 15$</p> <p>or SC1 for 18.36 or 0.85×21.60</p>	eg 10% = 2.16 and 5% = 1.06 and adding their values
	(b)		£6.63	2	<p>M1 for 0.13 or 13p or 6.5×1.02 or 6.5×0.02</p>	
	(c)		16 %	3	<p>M2 for $4 \div 25$ or 0.16 or $29 \div 25$ or 1.16 or $4 \div 0.25$ oe</p> <p>or M1 for 4 used or 1% of 25 = 0.25</p>	eg $4 \div 29$ 4 used could be $29 - 25$ as a numerator but an answer of 4% scores 0
2	(a)	(i)	5, 11	2	B1 for 5 or 11 or for -1 and 5 (using $n = 0$ and 1)	
		(ii)	16	3	<p>M2 for 16.8[333...] or $101/6$ seen or at least one value of n over 16 tried along with at least one below 16 (not 1 or 2)</p> <p>or M1 for $6n - 1 = 100$ or $6n - 1 < 100$ or at least two values of n tried (not 1 or 2)</p> <p>or SC2 for 17 following -1 and 5 in part (a)(i)</p> <p>After M0 award SC1 for answer of 17</p>	Solution by T&I is fine.

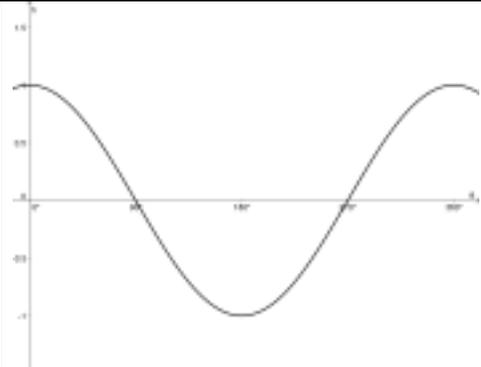
Question		Answer	Marks	Guidance
	(b)	$3n + 2$	2	M1 for $3n$
3	(a)	$\sqrt{2^2 + 3^2} = \sqrt{13} = 3.6(0555)$	3	M2 for $\sqrt{2^2 + 3^2}$ or M1 for $2^2 + 3^2$ or right angled triangle with 2 and 3 shown or Pythagoras using 2 and 3 and A1 for 3.60.....or 3.61 (at least 2dp)
	(b)	11.3 to 11.33	2	M1 for $3.1... \times 3.6$ or for $3.1... \times$ <i>their</i> (a)
4	(a)	-3.5 or -7/2 oe	2	M1 for $x + 5 = 1.5$ or $2x + 10 [=3]$ or FT their first step to a "correct" answer
	(b)	(i) $m = dv$	1	
		(ii) $b = \frac{2A}{h}$	2	Condone $b = A/0.5h$ or $b = A/1/2h$ M1 for $bh = 2A$ or $\frac{1}{2}b = \frac{A}{h}$ SC1 for $h = 2A/b$
5	(a)	26.5	2	M1 for $15.9 \div 6$ or $15.9 \div 3$ oe soi by 2.65 ($\times 10$) or 5.3 ($\times 5$)
	(b)	8	2	FT <i>their</i> 26.5 for M1 A1 M1 for $23 \div 2.65$ oe or 9 or 8.679... or $23 \div$ (<i>their</i> 26.5/10)
6	(a)	(i) 27.98[41] isw	1	Allow 28.0 but not 28

Question		Answer	Marks	Guidance
	(ii)	12 000	1	Allow answer in standard form
	(b)	35 : 38	2	M1 for division by 5 attempted or non-integer answers eg 87.5 : 95, 17.5 : 19, 1 : 1.08....., 0.921...: 1, etc.
7*		Correct answer (250) with complete correct working eg $(4 + 1) \times 5 \times 10$.	4	Working correctly communicated in stages is acceptable for 4 marks eg $4 + 1 = 5$, $5 \times 5 = 25$, $25 \times 10 = 250$. Full written explanation is also acceptable. 3: The working is correct but no final answer stated $(4 + 1) \times 5 \times 10$ or the working is poorly communicated but is clear eg $4 + 1 = 5 \times 5 = 25 \times 10 = 250$ or number greater than 200 with complete correct working. 2: 250 with no (or incomplete) working or for acceptable number over 200 with poorly communicated working 1: Acceptable number greater than 200 with no, or incomplete, working or for $(4 \times 5) \times 10$ [$\times 1$] condoning error in calculation or for two trials leading to numbers below 200 (condone poor communication). or acceptable calculation with their answer minimum 200 but error in evaluation 0: 200 with no working gets zero For 1 or 2 marks 'acceptable' implies number, minimum 200, that can be made.

Question		Answer	Marks	Guidance
8	(a)	$x = 20, y = 30$	5	<p>M2 for at least two of $x + 3y + 70 = 180$; $x = y - 10$; $3y + 70 + y - 10 = 180$ oe</p> <p>or</p> <p>M1 for one of these equations</p> <p>and</p> <p>M1 for getting a correct, simplified equation in just one variable eg $4y + 60 = 180$</p> <p>A1 $x = 20$ A1 $y = 30$</p>
	(b)	$c = 128\frac{4}{7}, d = 77\frac{1}{7}$ oe	5	<p>M1 for angle sum of heptagon or exterior angle of heptagon and M1 for $\text{sum} \div 7$ or $180 - \text{ext angle}$ and A1 exact angle c and M1 for use of isosceles triangle and A1 for angle d (can be decimal to at least 1dp – rounded or truncated)</p> <p>or</p> <p>B4 for answers of 128.6 and 77.2</p>
9		67.4	3	<p>M2 for $\tan^{-1} 14.4/6$ or</p> <p>M1 for $\tan R = \frac{14.4}{6}$ oe</p> <p>or</p> <p>M1 for use of their inverse trig function eg</p>

Question		Answer	Marks	Guidance	
11	(a)	Equation	1		
	(b)	Expression	1		
	(c)	Identity	1		
12	(a)	$6x^2 - x - 2$	3	<p>M2 for three of the following terms seen: $6x^2 - 4x + 3x - 2$ or M1 for two of the above terms</p>	<p>eg $6x^2 + 7x - 2$ or $6x^2 - 7x - 2$ or $6x^2 - x + 2$ could earn M2 (one error only)</p>
	(b)	$2(x - 2)(x + 2)$	2	<p>M1 for correct partial factorisation or SC1 for $(x - 2)(x + 2)$</p>	<p>eg $(2x - 4)(x + 2)$ or $2(x^2 - 4)$ or $(x - 2)(2x + 4)$</p>
	(c)	3, 0.5	3	<p>M2 for correct factors $(2x - 1)(x - 3)$ or M1 if <i>their</i> factors multiply to give two terms correct in the expansion or $(2x \pm 1)(x \pm 3)$ or $x(2x - 1) - 3(2x - 1)$ or B1 for one correct solution</p>	<p><u>Alternative:</u> ... use of formula M2 for correct substitution and simplification of formula to at least obtain $(7 \pm \sqrt{25})/4$ or M1 for substitution in formula with a maximum of two errors or ... completing the square M2 for correct completed square expression or M1 for correct squared bracket</p>

Question		Answer	Marks	Guidance	
13		$\frac{4}{33}$ or $\frac{12}{99}$ oe (must be fraction)	2	M1 for 0.12 or 0.1212 or $\frac{5}{11}$ oe	
14		HF = FJ sides of square GF = FE sides of square angle HFG = angle JFE = 90° or (vertically) opposite triangles are congruent SAS	3	M2 for all three statements with reasons or M1 for all three statements with no reason or for 2 statements with reasons and A1 for SAS (dep. on three statements with, or without, reasons)	After two correct sides given allow: GH = $\sqrt{(HF^2 + GF^2)}$ and EJ = $\sqrt{(FJ^2 + FE^2)}$ then SSS (or poss. RHS)
15	(a)	12.5	4	M3 for $m = 5\sqrt{p}$ or $5 \times \sqrt{6.25}$ or M2 for $k = 5$ or M1 for $m = k\sqrt{p}$ or $10 = k\sqrt{4}$ or SC1 for $m = 5p^2/8$ or $m = 20/\sqrt{p}$ and SC1 FT to 24.4.... or 8	For M1 condone $10 \propto k\sqrt{4}$
	(b)	400	2	M1 for $100 = 5\sqrt{p}$ FT from <i>their</i> formula, or <i>their</i> k, for M1 A1 (dep on formula involving either a square or a square root)	FT from SC in (a) to 12.6.. or 25

Question		Answer	Marks	Guidance	
16	(a)	8.37 to 8.38 isw	3	<p>M1 for 37.6 to 37.7 or $2 \times \pi \times 6$ and</p> <p>M1 for $\frac{80}{360}$ oe</p> <p>A1 8.37 to 8.38 or 8.4</p>	Answer to at least 1 dp or in terms of π (ie $8\pi/3$)
	(b)	77.1 to 77.3	4	<p>M1 for $2\pi r = \text{their (a)}$</p> <p>A1 FT for radius of base circle (r)</p> <p>M1 for $\cos \theta = \frac{\text{their}(r)}{6}$</p> <p>A1 77.1 to 77.3 or 77</p>	<p>(their(a))/2π soi by figs 1333.... 1.3333...</p> <p>Use of eg Pythagoras followed by sine rule – FT their (r) Use of radians leading to 1.3467...or gradians leading to 85.73379....scores M1 A1 M1</p>
17		 <p>Correct curve, reasonably smooth, between 0 and 360.</p>	2	<p>M1 for indication of correct turning points and intersections on x axis or for $\cos [\theta]$</p> <p>SC1 for reflection in $h = 0$ or sin curve</p>	eg allow M1 for $h = 1.5\cos\theta$ drawn

Question		Answer	Marks	Guidance	
18	(a)	40	2	M1 for $\frac{1}{3} \times 4^2 \times 7.5$	
	(b)	35	4	M1 for "pyramids similar" (may be implied by calculating corresponding lengths) M1 for length sf = 2 soi (eg by 3.75) M1 for vol sf = 8 seen or small pyramid vol = 5 (cm ³) oe	Vol. of small pyramid = 5 or $\frac{7}{8} \times \text{their (a)}$ implies first 3 marks. <u>Alternative:</u> It is possible to do this by splitting the frustum into a cuboid, 4 prisms and 4 pyramids. Allow B1 for each different correct volume: 15, 3.75, 1.25.

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