

**ADVANCED SUBSIDIARY GCE  
MATHEMATICS (MEI)**

**4755/01**

Further Concepts for Advanced Mathematics (FP1)

**MONDAY 2 JUNE 2008**

Morning  
Time: 1 hour 30 minutes

**Additional materials:** Answer Booklet (8 pages)  
Graph paper  
MEI Examination Formulae and Tables (MF2)

**INSTRUCTIONS TO CANDIDATES**

- Write your name in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Read each question carefully and make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- You are permitted to use a graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

**INFORMATION FOR CANDIDATES**

- The number of marks is given in brackets [ ] at the end of each question or part question.
- The total number of marks for this paper is 72.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.

This document consists of 4 printed pages.

## Section A (36 marks)

- 1 (i) Write down the matrix for reflection in the  $y$ -axis. [1]
- (ii) Write down the matrix for enlargement, scale factor 3, centred on the origin. [1]
- (iii) Find the matrix for reflection in the  $y$ -axis, followed by enlargement, scale factor 3, centred on the origin. [2]
- 2 Indicate on a single Argand diagram
- (i) the set of points for which  $|z - (-3 + 2j)| = 2$ , [3]
- (ii) the set of points for which  $\arg(z - 2j) = \pi$ , [3]
- (iii) the two points for which  $|z - (-3 + 2j)| = 2$  and  $\arg(z - 2j) = \pi$ . [1]
- 3 Find the equation of the line of invariant points under the transformation given by the matrix  $\mathbf{M} = \begin{pmatrix} -1 & -1 \\ 2 & 2 \end{pmatrix}$ . [3]
- 4 Find the values of  $A$ ,  $B$ ,  $C$  and  $D$  in the identity  $3x^3 - x^2 + 2 \equiv A(x - 1)^3 + (x^3 + Bx^2 + Cx + D)$ . [5]
- 5 You are given that  $\mathbf{A} = \begin{pmatrix} 1 & 2 & 4 \\ 3 & 2 & 5 \\ 4 & 1 & 2 \end{pmatrix}$  and  $\mathbf{B} = \begin{pmatrix} -1 & 0 & 2 \\ 14 & -14 & 7 \\ -5 & 7 & -4 \end{pmatrix}$ .
- (i) Calculate  $\mathbf{AB}$ . [3]
- (ii) Write down  $\mathbf{A}^{-1}$ . [2]
- 6 The roots of the cubic equation  $2x^3 + x^2 - 3x + 1 = 0$  are  $\alpha$ ,  $\beta$  and  $\gamma$ . Find the cubic equation whose roots are  $2\alpha$ ,  $2\beta$  and  $2\gamma$ , expressing your answer in a form with integer coefficients. [5]
- 7 (i) Show that  $\frac{1}{3r-1} - \frac{1}{3r+2} \equiv \frac{3}{(3r-1)(3r+2)}$  for all integers  $r$ . [2]
- (ii) Hence use the method of differences to find  $\sum_{r=1}^n \frac{1}{(3r-1)(3r+2)}$ . [5]

## Section B (36 marks)

8 A curve has equation  $y = \frac{2x^2}{(x-3)(x+2)}$ .

(i) Write down the equations of the three asymptotes. [3]

(ii) Determine whether the curve approaches the horizontal asymptote from above or below for

(A) large positive values of  $x$ ,

(B) large negative values of  $x$ . [3]

(iii) Sketch the curve. [3]

(iv) Solve the inequality  $\frac{2x^2}{(x-3)(x+2)} < 0$ . [3]

9 Two complex numbers,  $\alpha$  and  $\beta$ , are given by  $\alpha = 2 - 2j$  and  $\beta = -1 + j$ .

$\alpha$  and  $\beta$  are both roots of a quartic equation  $x^4 + Ax^3 + Bx^2 + Cx + D = 0$ , where  $A$ ,  $B$ ,  $C$  and  $D$  are real numbers.

(i) Write down the other two roots. [2]

(ii) Represent these four roots on an Argand diagram. [2]

(iii) Find the values of  $A$ ,  $B$ ,  $C$  and  $D$ . [7]

10 (i) Using the standard formulae for  $\sum_{r=1}^n r^2$  and  $\sum_{r=1}^n r^3$ , prove that

$$\sum_{r=1}^n r^2(r+1) = \frac{1}{12}n(n+1)(n+2)(3n+1). \quad [5]$$

(ii) Prove the same result by mathematical induction. [8]

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