

GCE

Further Mathematics B (MEI)

Y434/01: Numerical methods

Advanced GCE

Mark Scheme for Autumn 2021

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All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Annotations and abbreviations

Annotation in scoris	Meaning
√and ≭	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0,M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0,B1	Independent mark awarded 0, 1
Е	Explanation mark 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank page
Highlighting	
Other abbreviations in	Meaning
mark scheme	
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only previous M mark.
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
rot soi	Rounded or truncated Seen or implied
soi www	Rounded or truncated Seen or implied Without wrong working
soi	Rounded or truncated Seen or implied Without wrong working Answer given
soi www AG awrt	Rounded or truncated Seen or implied Without wrong working
soi www AG	Rounded or truncated Seen or implied Without wrong working Answer given

Q	uestion	1			Answer		Marks	AOs		Guidance
1	(a)	i	$\frac{1.414214 - }{\sqrt{2}}$	$\frac{7}{2}$ or $\frac{1.41421}{2}$	$\frac{4^2-2}{}$ oe s	oi	M1	1.1a	ignore modulus signs	
			0.000000	309449 is	W		A1	1.1	to 2 sf or more	
			0.000000	0618898 isv	w		A1	1.1	to 2 sf or more	
							[3]			
1	(a)	ii	the second error oe	l relative er	ror is doub	le the first relative	B1	2.2a		
							[1]			
1	(b)		Ben is wrong because the spreadsheet stores 1.414214 to a higher precision than is displayed (and so when the square of this number is calculated, 2 is returned) isw			B1	2.4	or 1.414214 is an approximation to $\sqrt{2}$ so 1.414214 ² \neq 2 oe		
							[1]			
2	(a)		2 3 4	f(x) -0.65 -0.35 1.77 5.71	Δ0.32.123.945.76	1.82 1.82	M1	1.1	finds 4 \(\Delta\) values, allow one error all correct	
							[2]			

	Question	Answer	Marks	AOs		Guidance
2	(b)	the second differences are constant oe	B1	1.1	allow the 3 rd differences are zero	
			[1]			
2	(c)	$-0.65 + 0.3(x-1) + 1.82 \times \frac{(x-1)(x-2)}{2!}$	M1	1.1	must be correct form; allow 1 substitution error	
		$[P_2(x) =] 0.91x^2 - 2.43x + 0.87$	A1	1.1	two of three terms correct	
			A1	1.1	all correct	
			[3]			
3	(a)	$\sinh x^2 - x^3 - 2 = 0$	B1	1.1	must see = 0	
			[1]			
3	(b)	=IF(H5>0,G5,E5)	B1	1.1	or =IF(H5<0,E5,G5)	must see =
			[1]			
3	(c)	1.48719×17.2899-2×-0.77825 17.28990.77825 0e	M1	3.1a	may be implied by 1.509	
		awrt 1.50928	A1	1.1	NB $f(1.50928) = -0.6111$ to 4 sf	
		awrt 1.52603	A1	1.1		
			[3]			

C	uestion	Answer	Marks	AOs		Guidance
3	(d)	the ratios are decreasing which suggests the convergence is (slightly) faster than 1st order	B1	2.2b	allow between 1st and 2nd order	do not allow eg not first order
		the ratios are close to 1 which suggests the convergence is slow	B1	2.2b		
			[2]			
4	(a)	$\frac{4.2472072-4}{0.1} \text{ or } \frac{4.0239468-4}{0.01} \text{ or }$ $\frac{4.0023871-4}{0.001} \text{ or } \frac{4.0002386-4}{0.0001}$	M1	3.1a	use of forward difference method	may be implied by one correct answer
		$2.472072 \qquad \text{(with } h = 0.1\text{)}$	A1	1.1	any two correct	
		2.39468 (with $h = 0.01$) 2.3871 (with $h = 0.001$)	A1	1.1	any three correct	
		2.386 (with $h = 0.0001$)	A1	1.1	all four correct	
			[4]			
4	(b)	comparison of last two estimates	M 1	1.1	if M0 allow SC1 for 2.39 is secure or	
		2.39 is secure or 2.386 is possible	A1	2.2b	2.386 is possible regardless of justification	
			[2]			
5	(a)	48×0.5 soi	M1	3.3		
		£24	A1	3.4		
			[2]			
5	(b)	consistent because 1.77 < 24	B1	2.4	allow consistent because error < mpe	
			[1]			

Q	Question	Answer	Marks	AOs		Guidance
5	(c)	52×0.495	M1	3.3		
		£25.74	A1	3.4		
			[2]			
5	(d)	this could happen if a large number of items eg cost less than £1 eg cost £1.99 or £2.99 etc eg more than 50p over the pound eg the mean error per item was 52.38p	B1	3.5a		
		3 1	[1]			
5	(e)	mpe = £0.99n	B1	3.4	condone omission of units, allow 99 <i>n</i> pence	
			[1]			
5	(f)	expected error for Nina's model is £0 since you would expect to round half the prices up and half down oe	B1	2.4		U6
		expected error in Kareem's model is $-£0.495n$ since you would expect the average "chop" to be 49.5p oe so new model should be "estimated cost" $+£0.495n$	B1	3.5c		

C	uestion	Answer	Marks	AOs		Guidance
			[2]			
6	(a)	$\frac{1}{2x} - 2x + 1 \text{ seen}$	M1	2.1		
		$x_{n+1} = x_n - \frac{0.5 \ln(x_n) - x_n^2 + x_n + 1}{\frac{1}{2x_n} - 2x_n + 1}$ oe soi	M1	1.1	may be implied by correct iterates	condone omission of subscripts
		1 3 2.0791668 1.7783346 1.7360141 1.7351281 1.7351277	M1	1.1	at least three further correct iterates derived from starting at 1 if $M0$ allow $SC1$ for 1.735128 from N-R method used with different x_0 and at least 3 correct iterates shown	correct to at least 5 sf where appropriate
		1.735128	A1	1.1		
			[4]			
6	(b)	3 2 1 C	M1	2.4	tangent at (1,1) (1,1) to (3,0)	
		-1 0 1 2 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	[2]	1.1	(1,1) to (3,0)	

Q	uestion	Answer	Marks	AOs		Guidance
6	(c)	N-R generally has 2 nd order convergence whereas fixed point iteration generally has 1 st order convergence	B1	2.4	allow eg N-R converges faster allow eg fixed point iteration more likely to fail oe	
			[1]			
6	(d)	ln(-0.403) is undefined (so the spreadsheet cannot compute a value)	B1	2.2a		
			[1]			
6	(e)	$\begin{array}{c} 0.5 \\ 1.0739769 \\ 1.4524673 \\ 1.6245304 \\ 1.6932631 \\ 1.7194743 \\ 1.7293015 \\ \end{array}$	M1	2.1 2.2a	need to see at least 3 iterates correct to at least 5 sf	
			[2]			

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	Question	Answer	Marks	AOs		Guidance
6	(f)	0.5 0.4764669 0.4528879 0.4293074 0.4057756 0.3823498 0.1116318 0.1111278 0.1110835 0.1110821 0.1110821	M1	1.1 2.2a	at least 3 correct iterates derived from starting at 0.5 if M0 allow SC1 for 0.111082 from relaxation method used with different x_0 and at least 3 correct iterates shown	iterates correct to at least 5 sf
			[2]			
7	(a)	$\frac{1}{16}$ isw or 0.0625 isw	B1	2.2a		
			[1]			
7	(b)	by comparison of T_{16} and T_{32} 0.6 is certain or 0.63 is probable	B1 [1]	2.2b		

C	Question	Answer	Marks	AOs		Guidance
7	(c)	r appears to be between 0.25 and 0.5	B1	2.2b		
		so order of convergence is between 1st and 2nd order	B1	2.2b		
		Alternative				
		$r > 0.25$ so convergence slower than 2^{nd} order	B1			
		r < 0.5 so convergence faster than 1st order	B1			
			[2]			
7	(d)	$\frac{2M_n+T_n}{3}$ or $\frac{4T_{2n}-T_n}{3}$ soi	M1	1.1		
		= $(2*O5 + N5)/3$ or = $(4*N6 - N5)/3$	A1	1.1	must see =	
			[2]			
7	(e)	awrt 0.62658745	B1	1.1		
		awrt 0.00029	B1	1.1		
		awrt 0.354	B1	1.1		
			[3]			

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Q	uestion	Answer	Marks	AOs		Guidance
7	(f)	S_{2n} and difference from table used in extrapolation	M1	3.1a	eg their 0.62658745 and their 0.00029	If M0 allow SC2 for awrt 0.626607 obtained
		awrt 0.62658745 and awrt 0.00029 used	A1	1.1	may see more dp for difference	from 16×0.62658745-0.62629755 15
		$0.62658745 + 0.00029 \times \frac{r}{1-r}$	A1	1.1	$0.35 \le r \le 0.36$	then SC1 for 0.627 obtained from comparison
		awrt 0.62674355 to awrt 0.62675058	A1	1.1		with S_{64}
		comparison with their S_{64} 0.6267 is secure	M1 A1	3.2a 2.2b	or 0.62675 is possible; allow 0.626746	
					the last two ${\bf A}$ marks are only available if answers obtained from extrapolation to infinity from S_{64}	
			[6]			

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