

GCE

Quantitative Methods (MEI)

Unit G244: Introduction to Quantitative Methods (MEI)

Advanced Subsidiary GCE

Mark Scheme for June 2015

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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Annotations and abbreviations

Annotation in scoris	Meaning
√and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in	Meaning
Other abbreviations in mark scheme	Meaning
Other abbreviations in mark scheme	Meaning Mark for explaining
Other abbreviations in mark scheme E1 U1	Meaning Mark for explaining Mark for correct units
Other abbreviations in mark scheme E1 U1 G1	Meaning Mark for explaining Mark for correct units Mark for a correct feature on a graph
Other abbreviations in mark scheme E1 U1 G1 M1 dep*	Meaning Mark for explaining Mark for correct units Mark for a correct feature on a graph Method mark dependent on a previous mark, indicated by *
Other abbreviations in mark scheme E1 U1 G1 M1 dep* cao	Meaning Mark for explaining Mark for correct units Mark for a correct feature on a graph Method mark dependent on a previous mark, indicated by * Correct answer only
Other abbreviations in mark scheme E1 U1 G1 M1 dep* cao oe	Meaning Mark for explaining Mark for correct units Mark for a correct feature on a graph Method mark dependent on a previous mark, indicated by * Correct answer only Or equivalent
Other abbreviations in mark scheme E1 U1 G1 M1 dep* cao oe rot	Meaning Mark for explaining Mark for correct units Mark for a correct feature on a graph Method mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated
Other abbreviations in mark scheme E1 U1 G1 M1 dep* cao oe rot soi	Meaning Mark for explaining Mark for correct units Mark for a correct feature on a graph Method mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied
Other abbreviations in mark schemeE1U1G1M1 dep*caooerotsoiwww	Meaning Mark for explaining Mark for correct units Mark for a correct feature on a graph Method mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working
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SUBJECT SPECIFIC MARKING INSTRUCTIONS

A Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

B An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

C The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an **M** mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Ε

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation *isw*. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- D When a part of a question has two or more 'method' steps, the **M** marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several **B** marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- E The abbreviation *ft* implies that the **A** or **B** mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, **A** and **B** marks are given for correct work only differences in notation are of course permitted. **A** (accuracy) marks are not given for answers obtained from incorrect working. When **A** or **B** marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, **A** marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow-through questions candidate-by-candidate rather than question-by-question.

F Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over-specified or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

G Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

H For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one **A** mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

C	Question		Answer	Marks	Guidance
1			Distance = $28 \times 60 \times 3 \times 10^8$ m	M1	
			$5040 imes 10^8 \mathrm{m}$	A1	Or equivalent
			$5.040 imes 10^8 ext{ km}$	B1	
			504 million km	B1	
			500 million to 1 significant figure	B1	
				[5]	
2	(i)		Immigration 1.85, Teenage mothers 5.33, Pensioners 2.18, Muslims 4.2, Religion 1.51	M1	
			Teenage mothers	A1	
_	([2]	
2	(ii)		There is no diagram/number showing actual for Germany Religion	B1	Confirm list of possible responses at SSU
			The numbers are the wrong way round for Australia Immigration	B1	
				[2]	

(Question		Answer	Marks	Guidance
3	(i)		Points plotted	B1	
			A smooth curve drawn	B 1	
				[2]	
3	(ii)		Tangent is drawn	B1	
			Year is about 2010	B1	Consistent with their graph
			Gradient of tangent is calculated	M1	
			Greatest increase is about 0.08 billion per year	A1	Accept 0.06 to 0.09 billion per year (Confirm range at SSU)
			$0.08 \ge 10^9 / 365 = 219\ 000$ people per day	B1	FT from previous answer
			No. This is difference between the number of babies born and the number of people dying per day.	B1	
				[6]	

0	Question		Answer	Marks	Guidance
4	(i)		20 years is 10 lots of 2 years	M1	Or equivalent
			$2^{10} = 1024$	A1	
			$1024 \approx 10^3$	B1	
				[3]	
4	(ii)		At least two points plotted correctly	B1	
			Four correct points joined to give the correct straight line	B1	
				[2]	
4	(iii)		It is a logarithmic scale	B1 [1]	
4	(iv)		50% increase is a factor of 1.5	M1	
			$1.5^2 = 2.25 \neq 2$ so this is not doubling	A1	
			Let <i>f</i> be the annual increase factor so $f^2 = 2$		
			$f = \sqrt{2} = 1.414$ So the annual increase is 41.4% and not 50%	E1	Or equivalent
4	(v)		$f^{35} = 1\ 000\ 000$	M1	
			$f = 1\ 000\ 000^{\frac{1}{35}}$	M1	
			f = 1.48 so the annual increase is 48%	A1 [3]	

Question		ion			Answer			Marks	Guidance
5	(i)		PATIENTS	Control Group Treatment as usual	New treatment Group			B2	1 mark for one correct entry, 2 marks for all three correct
			Improved	28	40				
			Not improved	38	31		_		
			Total	66	71	137			
5	(;;)							[2]	
	5 (11)		PROBABILITY	Control Group Treatment as usual	New treatm Group	ent		B2	1 mark for each correct table
			Improved	0.424	0.563				
			Not improved	0.576	0.437				
			Total	1	1				
								[2]	

Question		ion	Answer	Marks	Guidance
5	(iii)		It seems to have benefited some patients, but not all.	B1	Confirm acceptable responses at SSU
				[1]	
5	(iv)	(A)	$\frac{11}{16} = 0.6875$	B1	
		(B)	$\frac{7}{16} = 0.4375$	B1	
				[2]	
5	(v)		The new treatment might be harmful for less severely affected patients.	B1	Confirm acceptable responses at SSU
			The sample size was very small.	B1	
			Further tests should be carried out with larger numbers of patients.	B1	
				[3]	

Question				Answer						Marks	Guidance		
6	(i)		12	$120 \times \text{\pounds}8 = \text{\pounds}960, \ 100 \times \text{\pounds}10 = \text{\pounds}1000, \ 70 \times \text{\pounds}12 = \text{\pounds}840$									
					- 6 610	A1							
			A	A price of £10 gives the greatest income									
	(**)											[2]	
0	(II)		Pr	ice £8	gives unit p	rofit of £2 so c	overall pro	fit $120 \times \pounds$	$22 = \pounds 240$			IVI I	
			Th	ne ove	rall profit for	r f 10 is f 400 '	That for f	12 is f420					
			So	f_{12}	vives the gree	atest profit	1 nut 101 2	12 15 2 120	•			A1	
			50	/ 2 I 2 E	gives the grea	atest prom						[0]	
6	(iii)	(A)										[4]	Both answers required
U	(111)	(11)	Uni	t cost	Nearest 1p	Tota	al profit N	learest £1				B1	Doth unswers required
					_		_						
		(B)						1			1		
					Α	В	С	D	E	F			
				1	Unit sale	Number of	Unit	Unit	Total	Total			
					price	I-shirts	cost	profit	income	profit			
				5	£8	120	£3.76	£4.24	£960	£509		R 1	
												DI	
				•••									
				7	£10	100	£4	£6	£1000	£600		B2	
			•								-		

Question		ion	Answer	Marks	Guidance
		(C)	D2 = $A2 - C2$	B1	
			F2 = B2 * D2	B1	
				[6]	
6	(iv)		The best price is £10	B1	FT from their answers in spreadsheet
				[1]	L

C	Question		Answer	Marks	Guidance
7	(i)		Normal curve Shape	B1	
			Mean	B1	
			Realistic spread	B1	
				[3]	
7	(ii)		The wind speed is never negative	B1	
				[1]	
7	(iii)		9 m s^{-1} is 2 standard deviations from the mean	M1	
			95% lies within 2 standard deviations so 5% is outside	A1	
			So 2.5% at each side. The wind should be above 9 m s ⁻¹ for 2.5% of the time	A1	
				[3]	
7	(iv)		2.05 + 1.01 + 0.51 + 0.25 + 0.12 + 0.05 + 0.02 + 0.01	M1	
			= 4.02%	A1	
				[2]	
7	(v)		It is not quite Normal but not far off either.	B1	
				[1]	
7	(vi)		The numbers should be at the ends of the intervals	B1	
			The bars should cover the full width of the intervals	B1	
1				[2]	

Question		ion	Answer	Marks	Guidance
8	(i)	(A)	To go from UK to USA sizes, subtract 4	B1	
		(B)	To go from UK to France sizes, add 28	B1	
				[2]	
8	(ii)	(A)	$w = 76 \implies S = \frac{2}{5} \times (76 - 41) = 0.4 \times 35 = 14$ as required	B1	
		(B)	$w = 73 \Longrightarrow S = \frac{2}{5} \times (73 - 41) = 0.4 \times 32 = 12.8$	B1	
			Round to nearest even number	B1	
		(C)	$F = \frac{2}{5}(w - 41) + 28$	M1	
			$F = \frac{2}{5} \left(w + 29 \right)$	A1	
			$F = \frac{2}{5} (81 + 29) = 44$	A1	
				[6]	
8	(iii)		In Japan 61 cm is size 7, 66 cm is size 9 etc	B1	
			So subtract 3 to find the USA equivalent	B1	
				[2]	

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