Foundation Check In - 9.01 Plane isometric transformations

**For questions 1-2, use the diagram below.**



1. Shape A is rotated onto shape B. What are the coordinates of the centre of rotation?

A

1. Shape A is rotated onto shape C. What are the coordinates of the centre of rotation?

C

**For questions 3-5, use the diagram below.**



1. Shape D is reflected onto shape E. What is the equation of the mirror line?

D

1. Shape E is reflected onto shape G. What is the equation of the mirror line?

F

1. Shape E is reflected onto shape F. What is the equation of the mirror line?

**For questions 6-8, use the diagram below**.



1. Use a column vector to describe the translation that maps shape H onto shape J.

H

1. Fully describe the transformation that maps shape I onto shape K.
2. Fully describe the transformation that maps shape H onto shape I.

K

1. Kara draws a triangle with vertices at (3, 1), (6, 2) and (3, 3). She reflects this triangle in the line . What are the coordinates of the vertices of the reflected triangle?
2. A triangle with vertices at (1, 2), (5, 2) and (5, 4) is reflected in the line . The original triangle and its reflection combine to form a new triangle which is isosceles. Work out the area of the isosceles triangle.

**Extension**

Nigel has 20 white tiles and 4 black tiles. Each of his tiles are square and the same size as each other.

He plans to create a tile design in the shape of a square made up of 16 tiles. He wants the design to have a vertical line of symmetry.

One example design, using 12 white tiles and all 4 black tiles, is shown to the right.

How many different tile designs can Nigel make?

Answers

1. (1, 1)
2. (-1, 0)
3. 
4. 
5. 
6. Translation 
7. Reflection in .
8. Rotation about (2, 1) by 90° clockwise (or 270° anticlockwise).
9. A diagram could be used, however reflection in  implies the *y*-coordinate of each vertex becomes the *x*-coordinate (and vice-versa). The coordinates are (1, 3), (2, 6) and (3, 3) with the final vertex being unchanged by the reflection.
10. The original triangle has a horizontal base length of 4 units and a vertical height of 2 units, so its area is  units2. Since the isosceles triangle is formed from the original triangle and its reflection, the area of the isosceles triangle will be double that of the original triangle. Therefore the area is 8 units2.

**Extension**

Since the design needs to have a line of symmetry, whatever Nigel does on the left of the “mirror line” will need to be reflected in the right. He is limited by having 4 black tiles and so at most 2 of these can be on the left of the mirror line (since 2 would then need to be on the right, using up all 4 black tiles).

We therefore consider how many ways he can use up to 2 black tiles on the 2 × 4 grid to the left of the mirror line.

Firstly, with no black tiles (and 8 white) there is only one design he can make.

With 1 black tile (and 7 white), there are 8 positions it could go in, so 8 possible designs with 1 black tile.

With 2 black tiles (and 6 white), there are 8 positions the first tile could go in. For each of these, there are only 7 remaining choices for where the second tile could go. But half of these would be duplicates: for example in the diagram below, the 1 and 2 indicate which tile is placed first and second.

 

But these lead to the same design (we don’t care about which one is placed first), so we only need to consider half of the  ways of placing the two black tiles, i.e. 28 designs are possible with 2 black tiles.

Altogether there are  different designs that Nigel could make.

We’d like to know your view on the resources we produce. By clicking on ‘Like’ or ‘Dislike’ you can help us to ensure that our resources work for you. When the email template pops up please add additional comments if you wish and then just click ‘Send’. Thank you.

Whether you already offer OCR qualifications, are new to OCR, or are considering switching from your current provider/awarding organisation, you can request more information by completing the Expression of Interest form which can be found here: [www.ocr.org.uk/expression-of-interest](http://www.ocr.org.uk/expression-of-interest)

Looking for a resource? There is now a quick and easy search tool to help find free resources for your qualification:
[www.ocr.org.uk/i-want-to/find-resources/](http://www.ocr.org.uk/i-want-to/find-resources/)

**OCR Resources**: *the small print*OCR’s resources are provided to support the delivery of OCR qualifications, but in no way constitute an endorsed teaching method that is required by the Board, and the decision to use them lies with the individual teacher. Whilst every effort is made to ensure the accuracy of the content, OCR cannot be held responsible for any errors or omissions within these resources. This formative assessment resource has been produced as part of our free GCSE teaching and learning support package. All the GCSE teaching and learning resources, including delivery guides, topic exploration packs, lesson elements and more are available on the qualification webpages. If you are looking for examination practice materials, you can find Sample Assessment Materials (SAMs) and Practice Papers on the qualification webpage <http://www.ocr.org.uk/qualifications/gcse-mathematics-j560-from-2015/>

© OCR 2018 - This resource may be freely copied and distributed, as long as the OCR logo and this message remain intact and OCR is acknowledged as the originator of this work.

OCR acknowledges the use of the following content: n/a

Please get in touch if you want to discuss the accessibility of resources we offer to support delivery of our qualifications: resources.feedback@ocr.org.uk

To give us feedback on, or ideas about the OCR resources you have used, email resourcesfeedback@ocr.org.uk

To give us feedback on, or ideas about the OCR resources you have used, email resourcesfeedback@ocr.org.uk

To give us feedback on, or ideas about the OCR resources you have used, email resourcesfeedback@ocr.org.uk

To give us feedback on, or ideas about the OCR resources you have used, email resourcesfeedback@ocr.org.uk

To give us feedback on, or ideas about the OCR resources you have used, email resourcesfeedback@ocr.org.uk

To give us feedback on, or ideas about the OCR resources you have used, email resourcesfeedback@ocr.org.uk

**OCR Resources**: *the small print*OCR’s resources are provided to support the teaching of OCR specifications, but in no way constitute an endorsed teaching method that is required by the Board, and the decision to use them lies with the individual teacher. Whilst every effort is made to ensure the accuracy of the content, OCR cannot be held responsible for any errors or omissions within these resources.
© OCR 2014 - This resource may be freely copied and distributed, as long as the OCR logo and this message remain intact and OCR is acknowledged as the originator of this work.

**OCR Resources**: *the small print*OCR’s resources are provided to support the teaching of OCR specifications, but in no way constitute an endorsed teaching method that is required by the Board, and the decision to use them lies with the individual teacher. Whilst every effort is made to ensure the accuracy of the content, OCR cannot be held responsible for any errors or omissions within these resources.
© OCR 2014 - This resource may be freely copied and distributed, as long as the OCR logo and this message remain intact and OCR is acknowledged as the originator of this work.

OCR acknowledges the use of the following content::
⚫ Garden: Elen Eliseeva/Shutterstock.com ⚫ Flag: Pixel Europe/Shutterstock.com

To give us feedback on, or ideas about the OCR resources you have used, email resourcesfeedback@ocr.org.uk

|  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| **Assessment Objective** | **Qu.** | **Topic** | **R** | **A** | **G** |  | **Assessment Objective** | **Qu.** | **Topic** | **R** | **A** | **G** |
| AO1 | 1 | Identify the centre of rotation of a triangle under rotation |  |  |  |  | AO1 | 1 | Identify the centre of rotation of a triangle under rotation |  |  |  |
| AO1 | 2 | Identify the centre of rotation of a triangle under rotation |  |  |  |  | AO1 | 2 | Identify the centre of rotation of a triangle under rotation |  |  |  |
| AO1 | 3 | Identify vertical mirror line and state its equation |  |  |  |  | AO1 | 3 | Identify vertical mirror line and state its equation |  |  |  |
| AO1 | 4 | Identify horizontal mirror line and state its equation |  |  |  |  | AO1 | 4 | Identify horizontal mirror line and state its equation |  |  |  |
| AO1 | 5 | Identify mirror line and state its equation |  |  |  |  | AO1 | 5 | Identify mirror line and state its equation |  |  |  |
| AO2 | 6 | Use a column vector to describe a translation of a simple shape |  |  |  |  | AO2 | 6 | Use a column vector to describe a translation of a simple shape |  |  |  |
| AO2 | 7 | Fully describe reflection, identifying a mirror line and state its equation |  |  |  |  | AO2 | 7 | Fully describe reflection, identifying a mirror line and state its equation |  |  |  |
| AO2 | 8 | Fully describe rotation, identifying the centre, angle and direction |  |  |  |  | AO2 | 8 | Fully describe rotation, identifying the centre, angle and direction |  |  |  |
| AO3 | 9 | Solve a problem involving reflection |  |  |  |  | AO3 | 9 | Solve a problem involving reflection |  |  |  |
| AO3 | 10 | Solve a problem involving reflection and area |  |  |  |  | AO3 | 10 | Solve a problem involving reflection and area |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| **Assessment Objective** | **Qu.** | **Topic** | **R** | **A** | **G** |  | **Assessment Objective** | **Qu.** | **Topic** | **R** | **A** | **G** |
| AO1 | 1 | Identify the centre of rotation of a triangle under rotation |  |  |  |  | AO1 | 1 | Identify the centre of rotation of a triangle under rotation |  |  |  |
| AO1 | 2 | Identify the centre of rotation of a triangle under rotation |  |  |  |  | AO1 | 2 | Identify the centre of rotation of a triangle under rotation |  |  |  |
| AO1 | 3 | Identify vertical mirror line and state its equation |  |  |  |  | AO1 | 3 | Identify vertical mirror line and state its equation |  |  |  |
| AO1 | 4 | Identify horizontal mirror line and state its equation |  |  |  |  | AO1 | 4 | Identify horizontal mirror line and state its equation |  |  |  |
| AO1 | 5 | Identify mirror line and state its equation |  |  |  |  | AO1 | 5 | Identify mirror line and state its equation |  |  |  |
| AO2 | 6 | Use a column vector to describe a translation of a simple shape |  |  |  |  | AO2 | 6 | Use a column vector to describe a translation of a simple shape |  |  |  |
| AO2 | 7 | Fully describe reflection, identifying a mirror line and state its equation |  |  |  |  | AO2 | 7 | Fully describe reflection, identifying a mirror line and state its equation |  |  |  |
| AO2 | 8 | Fully describe rotation, identifying the centre, angle and direction |  |  |  |  | AO2 | 8 | Fully describe rotation, identifying the centre, angle and direction |  |  |  |
| AO3 | 9 | Solve a problem involving reflection |  |  |  |  | AO3 | 9 | Solve a problem involving reflection |  |  |  |
| AO3 | 10 | Solve a problem involving reflection and area |  |  |  |  | AO3 | 10 | Solve a problem involving reflection and area |  |  |  |