

Cambridge Technicals

Engineering

Unit 1: Mathematics for Engineering

Level 3 Cambridge Technical Certificate/Diploma in Engineering
05822 - 05825

Mark Scheme for June 2017

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, Cambridge Nationals, Cambridge Technicals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

© OCR 2017

Subject-specific marking instructions

Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. These annotations must be in the body of the work and **not** anywhere near the right hand margin of each page.

Mark in using a red pen.

Put the mark for each subquestion near to and to the right of the mark for the question. Total all marks for the question and put this total in a ring at the bottom right of each question.

Transfer these marks to the box on the front page.

Total the marks for the paper. I suggest that all unringed marks are then totalled to make sure that the final mark is correct.

An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

DM

A method mark which is dependent on a previous method mark.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate. This will generally be achieved by withholding the last A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

Question		Answer	Marks	Guidance
1	(a)	$\Rightarrow 2x + 4 = 14$ $\Rightarrow 2x = 10$ $\Rightarrow x = 5$	M1 A1 A1	Remove brackets (i.e. sight of $2x + 4$ or $2x - 1$) Collect terms together Accept $x = 5$ www for 3 marks
			[3]	
	(b)	$\frac{2x+1}{3} + \frac{3x-2}{6} = \frac{4x+2}{6} + \frac{3x-2}{6}$ $= \frac{7x}{6} \text{ oe}$	M1 A1 A1	Sight of 6 (or multiple of 6) as common denominator Correct numerators
			[3]	
	(c)	$\Rightarrow T^2 = \frac{4\pi^2 L}{g}$ $\Rightarrow L = \frac{gT^2}{4\pi^2} \text{ oe}$	M1 M1 A1	Square both sides Make L the subject $L = \frac{gT^2}{2\pi^2}$ is M1 M1 A0
			[3]	
	(d) (i)	Long division or “build up” method	M1 A1	Evidence of multiplication (includes a 2×2 table) All algebra correct
			[2]	
	(ii)	$x^2 + x - 12 = (x \pm 4)(x \pm 3)$ $\Rightarrow (f(x)) = (x - 1)(x + 4)(x - 3)$	M1 A1	Evidence of attempt to factorise soi All algebra correct isw
			[2]	

Question			Answer	Marks	Guidance
2	(a)	(i)	$k = 20$ It represents the initial voltage	B1 B1	(award if seen in (ii).) Or voltage at $t = 0$ Accept "Peak voltage" or "highest voltage"
				[2]	
	(a)	(ii)	$1 = 20e^{3a} \Rightarrow 3a = \ln 0.05$ $\Rightarrow a = \frac{1}{3} \ln 0.05 = -0.999 \approx -1$	M1 M1 A1	Use of logs Correct substitution of 3 and 1 using <i>their k</i>
				[3]	
	(b)		Straight line Through origin	B1 B1	Give this mark even if you cannot award the first one
				[2]	
	(c)	(i)	$\left(\frac{2+6}{2}, \frac{5+9}{2}\right) = (4, 7)$	M1 A1	Attempt to find mean of values soi by sight of 4 or 7
				[2]	
	(c)	(ii)	$g = \frac{9-5}{6-2} = 1$	M1 A1	Change in y over change in x Accept ans of 1 www for 2 marks
				[2]	
	(c)	(iii)	$y = \textit{their g} x + \textit{anything}$ Or $y = \textit{anything} x + 3$ $y = x + 3$	B1 B1	For both: Ans has 3 terms only
				[2]	

Question		Answer	Marks	Guidance	
3	(i)	Large rectangle = $(7 + 2x)(4 + 2x) = 28 + 22x + 4x^2$ \Rightarrow Surround = $28 + 22x + 4x^2 - 28$ $= 4x^2 + 22x$	M1	Large rectangle minus small rectangle	Or any acceptable method of splitting the surround into rectangles and squares
			A1		
			A1	N.B. AG so working must be seen	
			[3]		
	(ii)	$4x^2 + 22x = 42$ $\Rightarrow 2x^2 + 11x - 21 = 0$ $\Rightarrow (2x - 3)(x + 7) = 0$ $\left(\text{or } x = \frac{3}{2} \text{ and } x = -7 \right)$ $\Rightarrow x = \frac{3}{2} \quad \text{oe}$	B1	Correct quadratic equation	
			M1	Solve <i>their</i> quadratic by correct formula or factorisation or completing the square	
			A1	2 roots or factors soi	
			A1	($x = -7$ can be discarded anywhere but it must be discarded)	Alternative: Trial and error B4
			[4]		

Question		Answer	Marks	Guidance
4	(a)		B1 B1 B1	Each graph correct and clearly labelled S.C. All 3 correct but none labelled B1
			[3]	
	(b)	(i)	$BM^2 = 2^2 + 1^2 = 5$ $\Rightarrow BM = \sqrt{5}$	M1 A1 Pythagoras Accept 2.2, 2.23, 2.24, 2.236....
			[2]	
	(b)	(ii)	Angle BMA = Angle CMD = $\tan^{-1} 2 = 63.4^\circ$ \Rightarrow Angle BMC = $180^\circ - 2 \times 63.4^\circ = 53.1^\circ$ Alternatively Drop perpendicular to BC from M giving half the angle $\tan^{-1} 0.5 = 26.6$ B1 Giving angle 53.1 B1 Alternatively: Use of triangle BMC and sin Alternatively use correct cosine rule Alternatively: use areas	B1 B1 Sight of 63.4
			[2]	
	(b)	(iii)	$\text{Arc length} = 2\pi \times MB \times \frac{53}{360}$ $= 2.07\dots$	M1 A1 Correct formula using <i>their</i> MB and 53 or <i>their</i> 53 Anything that rounds to 2.1 www
			[2]	

Question		Answer	Marks	Guidance
5	(i)	$\text{Area} = \int_0^8 (x^2 - 8x + 21) dx = \left[\frac{x^3}{3} - 4x^2 + 21x \right]_0^8$ $= \left(\frac{512}{3} - 256 + 168 \right) - (0) = \frac{248}{3}$	M1 A1 M1 A1	Evidence of integration (all powers increased by 1 but beware multiplication by x .) All three terms (ignore limits) Limits applied correctly Accept 82.6 or anything that rounds to 82.7 isw (i.e. taking 82.7 from 21×8)
			[4]	
	(ii)	$\frac{dy}{dx} = 2x - 8$ $= 0 \text{ when } x = 4$ $\Rightarrow y = 5$ Coordinates of D are (4, 5)	M1 M1 A1 A1	Diffn Set = 0 x y
			[4]	

Question			Answer	Marks	Guidance
6	(a)	(i)	P(red) = 0.6 or (30/50) P(both red) = $(0.6)^2 = 0.36$ (or $\frac{9}{25}$)	B1 B1	S.C. P(both blue) = 0.16 oe B1
				[2]	
	(a)	(ii)	P(both red) = $\frac{30}{50} \times \text{anything}$ 2nd fraction = $\frac{29}{49}$ P(both red) = $\frac{30}{50} \times \frac{29}{49} = \frac{87}{245} \approx 0.355$	M1 A1 A1	Treat P(both blue) as MR S.C. $\frac{29}{49}$ seen anywhere B1
				[3]	
	(b)	(i)	Median is 16 th value (or 16.5th value) = 2	M1 A1	Accept 2 www for 2 marks
				[2]	
		(ii)	Mode = 2	B1	
				[1]	
		(ii)	Positive skew, or skewed to the right Explanation	B1 B1	Accept "left skew" (only award if there is a description) e.g. more data to the left longer tail to the right most machines have a small number of reusable boards data loaded towards zero Curves down in the positive direction
				[2]	

OCR (Oxford Cambridge and RSA Examinations)
1 Hills Road
Cambridge
CB1 2EU

OCR Customer Contact Centre

Education and Learning

Telephone: 01223 553998

Facsimile: 01223 552627

Email: general.qualifications@ocr.org.uk

www.ocr.org.uk

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored

Oxford Cambridge and RSA Examinations
is a Company Limited by Guarantee
Registered in England
Registered Office; 1 Hills Road, Cambridge, CB1 2EU
Registered Company Number: 3484466
OCR is an exempt Charity

OCR (Oxford Cambridge and RSA Examinations)
Head office
Telephone: 01223 552552
Facsimile: 01223 552553

© OCR 2017

