

GCE

Mathematics

Unit 4736: Decision Mathematics 1

Advanced Subsidiary GCE

Mark Scheme for June 2017

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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These are the annotations, (including abbreviations), including those used in scoris, which are used when marking

Annotation in scoris	Meaning
√and ≭	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
Λ	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
M1 dep*	Method mark dependent on a previous mark, indicated by *
сао	Correct answer only
Oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

Here are the subject specific instructions for this question paper

a Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Mark Scheme

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

c The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Mark Scheme

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.
- g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

MARK SCHEME

Question		on	Answer/Indicative content	Mark	Guidance
1	(i)				(Lists may be written vertically)
			After 1 st pass 10 3 6 12 4 5 12	M1	First pass has 12 at right-hand end (even if other values are wrong)
			After 2^{nd} pass 3 6 10 4 5 12 12		(first row or first row after original or identified as pass 1)
			After 3^{rd} pass 3 6 4 5 10 12 12	A1	This list after 3 rd pass (even if there were earlier errors)
			After 4^{th} pass 3 4 5 6 10 12 12		
			After 5 th pass 3 4 5 6 10 12 12	B1	List sorted after 4 th pass, 5 th pass used to check but no 6 th pass
				[3]	
	(ii)	(a)	40 27 8 14	B1	This list (first or second)
			27 40 8 14	B1	This list (first or second)
			Note: given list was 27 8 14 40, this may appear before the		If more than two lists are given, mark the first two only
			answers		
				[2]	
		(b)	2	B1	'2 more'
					Ignore any passes shown, B1 is for stating that there are two (more)
				[1]	

2					Must be written answers.
					Diagrams may support reasoning but get no marks on their own.
	(i)	(a)	The nodes are not all of even order.	B1	It has an odd vertex; it has odd vertices; it has a vertex of order 5
					which is odd
				[1]	Need 'odd' (or 'not all even'), not just 'there is a vertex of order 5'
		(1-)			Lleing 'arrent and a franting with add water and a' to do have
		(D)	Use other is even (hence evently 2 nodes of odd order so semi	BI	Using even number of vertices with odd vertex order to deduce that there are 2 add vertices (or only one of the missing ones is add)
			Eulerian)		need not explicitly say 'so semi Eulerian'
			OR		Not just stating that there must be 2 odd vertices (or that one of the
			Total vertex order is even so one more odd node (one odd and		missing ones is odd) (with or without reference to semi-Eulerian)
			one even) (exactly one extra odd) (2 odd nodes altogether)		Not for calculating the missing orders 1. 2 or for using total = 16
				[1]	
	(ii)				Answer must be labelled as (ii) not credited in (iii)
			The sum of the vertex orders = 2×10^{-10} x number of arcs	M1	Sum of orders = 16 or twice number of arcs or sight of $2 \times 8 = 16$
			= 16		or sum of missing orders = $3 \text{ or } 16 - (2+2+4+5) \text{ or } 16 - 13$
			\Rightarrow missing orders sum to 3		or use reasoning similar to (iii) using vertex of order 5
					Not just from a diagram and not from unsupported answers 1 and 2
			Simply connected so vertex order 0 is impossible	Δ1	Missing orders are 1 and 2 (deduced from a complete and correct
			Hence missing vertex orders are 1 and 2	711	reasoned argument including simply connected or $16 - 13$)
				[2]	reasoned argument meridaning simply connected of 10 (15)
	(iii)		Given a simply connected graph vertex orders 5, 4, 2, 2, 2, 1		Do not need to explain why these are the vertex orders
					Accept other words for 'order' provided intention is obvious
			The vertex of order 5 must be joined to each of the others	D1	Understanding connections for the vertex of order 5
			The vertex of order 5 must be joined to <u>each</u> of the others	DI	Orderstanding <u>connections</u> for the vertex of order 5
			The order 4 is also connected to the three 2's	M1	Trying to deal with <u>connections</u> for the other vertices,
			The order 1 is not connected to any of these		any one of these three statements or equivalent
			The order 2's are not connected to each other		(e.g. order 4 is connected to three others)
			Hence, all such graphs have the same structure (are isomorphic)	Δ1	Correct argument from a simply connected graph with vertex orders
			Thence, an such graphs have the same structure (are isomorphic)	AI	5 4 2 2 2 1 to only one possible structure
				[3]	5, 1,2,2,2,1 to only one possible structure
	1	1		L- J	

Mark Scheme

3	(i)									Mark entries in columns for the variables: N, P, M, A, B in the row
	~ /	Line	N	Р	М	A	В	Display		where they first appear
		10	5					J J		Ignore any row labelled as line 20 or line 60
		80	5	0	5				B1	Line 10. $N = 5$
		00		0	5	13			B1	P = 0 and $M = 5$ both on second row
		100				15	12		M1	A = 13 on the next row
		110					12	5 10 12	Al	B = 12 on the following row and stopping after (attempted) display
		110						5, 12, 15	111	B = 12 on the following fow and stopping after (attempted) display
										Ignore values copied down into lower rows
										Do not deduce entries from printed display values
										Do not deddee entries nom printed display valdes
									[4]	
	(ii)					•				Mark entries in columns for the variables: <i>N</i> , <i>P</i> , <i>M</i> , <i>A</i> , <i>B</i> in the row
		Line	N	P	М	A	В	Display		where they first appear
		10	20							Ignore any row labelled as line 20 or line 60
		30		1					B1	Line 10, $N = 20$
		40			20					
		50			10				B1	P = 1 with $M = 10$ (second and fourth rows)
		70		2					B1	P = 2 with $M = 5$ (fifth and sixth rows)
		50			5					
		90			0	52			M1	A = 52 on the next row
		100					48		A1	B = 48 on the following row and stopping after (attempted) display
		110					10	20 48 52		
		110						20, 40, 52		Ignore values copied down into lower rows
										Do not deduce entries from printed display values
									[5]	
	(iii)	$N=2^x$ wi	ll be re	epeated	ly halv	ed unti	M = 1		M1	Iterate <u>until</u> it = 1, may be from trying a specific case or implied
		and $P = x$	C						A1	P = x, may be deduced from specific cases but need x here
										$[P = x + 1 \Rightarrow M1, A0] [P = x \Rightarrow M1, A1]$
		Then $A =$	$2 \times 2^{x-1}$	$=2^{x}$ (c	or $A = N$	V)			B1	$A = 2^x$ or $A = N$ (but not $A = 2^p$)
		and $B = 2$	$2^{x} - 2^{x} =$	= 0					B1	B=0
		The displ	ayed v	alues (for N, E	(B, A) ar	$e 2^x, 0,$	2^{x}		This B1 B1 may be implied from these displayed values in this form
		1	2			-				and in this order
									[4]	

4	(i)	B and E	B1 Both correct and no others
			May list vertex orders but need B and E specifically identified
			[1]
	(ii)	A - D - F = 13 + 16 = 29	M1 Evidence of considering both $A - D - F$ and $A - E - F$
		A - E - F = 27 + 8 = 35	or sight of both 35 and 29 or mentioning both D and E
		Shortest travel time = 29 minutes	A1 29, after considering <u>both</u> possibilities
			SC1 for 29 without showing evidence of considering alternatives
			[2]
	(iii)		M1 Correct temporary labels (with no extras) at <i>A</i> , <i>C</i> and <i>D</i>
		A 2 6 B 1 0 C 5 19	(may imply temporary label at A if permanent label = 6 but not for C
		6 19	and D)
		D 3 7 E 8 24 F 7 23	M1 dep Some updating of (their) temporary values at <i>E</i> only
		7 33 24 23	No penalty for crossing out e.g. 33 provided it is evident that a value
			has been updated in the lower box for E (and nowhere else, i.e. no
		G 6 20 H 4 18	Al updating at F, G, H
		20 18	All permanent labels correct (not implied from temporary labels)
			Order of labelling correct for their permanent labels (using their
			order gives their permanent labels listed in increasing order)
			If any permanent label is missing there should be no order label
	()	Total time for direct routes 222	[4] M1 Attempt at total for helf of table is 222 or 444 : 2
	(1V)	1 otal time for direct routes = 222	MI Attempt at total for <u>nair</u> of table i.e. 222 of $444 \div 2$
		then repeat B to $E = 24$	$A1 \qquad 246 = A1 = 266 = C = \frac{1}{2} $
		10tat time = 240 minutes	A1 246 of 4 nours 6 minutes (cao) [answer 246 o.e. \Rightarrow M1, A1]
		Repeated arcs BC and CE	B1 Accort P C E (correct not f) but not a σ ' P E via C'
		C is travelled through A times	B1 Accept $D = C = E$ (correct, not it) but not e.g. $D = E$ via C B1 A or $2 + 1 = 4$
		C is travened through 4 times	$\begin{bmatrix} D_1 \\ 4 & 0 & 0 \\ 1 & 1 \end{bmatrix} = 4$

5	(i)	P-J-N-M-L-K-P	M1	Route starts $P - J - N - M$
		6 + 5 + 6 + 11 + 12 + 8 = 48 miles	A1	48
		0 + 0 + 0 + 11 + 12 + 0 + 10 111105	[2]	
	(ii)	e.g. $P-L-M-N-J-K-P$ or $P-M-N-J-K-L-P$	M1	One of these routes. or in reverse
		= 46 miles $= 47$ miles	A1	Correct length (46 or 47) for their route (having achieved M1)
			[2]	
	(iii)	JN = 5 $J = K$		JN may be written as NJ, etc. Need not see individual weights
		JP = 6	M1	At least five of these seven arcs written listed by increasing order of
		MN = 6		weight, may have MN before JP and/or MP before KP
		$JK = 7$ $N \checkmark$ Weight = 33		Not just a list of weights and not from diagram
		$\frac{KP=8}{2}$	A1	Indicating that KP and MP are not chosen
		MP = 8		
		LP = 9 M L	B1	Correct tree
			B1	33 (miles)
			[4]	
	(iv)	<i>k</i> > 9	B1	k greater than 9 (not $k \ge 10$ and not $k \ge 9$)
		<i>LM</i> must be longer than both <i>LP</i> and <i>MN</i> , and the longer of these	B1	LP = 9 and $MN < 9$, need to explicitly refer to both LP and MN
		1S $LP = 9$	[0]	(i.e. least weight arc at each end of new arc)
	()	Charlest along that have not seen and IM's	[2]	
	(V)	Shortest closed route that does not use arc LM is D = M = N = L = D (ar in reverse) = 47 miles	M1	(Chartest route without IM has langth) 47 (aci)
		P - M - N - J - K - L - P (or in reverse) = 47 mines	IVII	(Shortest route without LM has length) 47 (sol)
		Shortest route that does use arc IM is	M1	(Shortest route using IM has length) $35 \pm k$ (soi)
		Shortest route that does use are Livits P = I = M = N = I = K = P (or in reverse) = 35 + k miles	1011	(Shortest route using Lin has length) $55 \pm k$ (sol)
		I = L in I = J in I =		
		So $35 \pm k < 47 \rightarrow k < 12$ (hence $9 < k < 12$)	A1	k < 12 (not $k < 11$ not $k = 10, 11$ and not $k < 12$)
		$50.55 + k < 47 \rightarrow k < 12 (hence) < k < 12)$		[from either M mark]
		For reference		
		J 7 K		SC1 for $k < 12$ (with or without reference to <i>LK</i>)
				(or as part of a double inequality, e.g. $9 < k < 12$)
				if neither M mark has been given
		N		
		6 /8 9		
			[3]	
		M L		

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6	(i)			M1	Any one coordinate correct
			A = (0, 4) $B = (0, 2)$	A1	(0, 4) and $(0, 2)$ both correct
			C = (4, 1) $D = (4, 3)$	A1	(4, 1) and (4, 3) both correct
			E = (3, 5)	A1	(3, 5) correct
					Ignore not labelling as A, B, C, D, E or mislabelling
				[4]	
	(ii)		Either checking vertices or using a sliding profit line	M1	Sight of any $3x + 13y$ for specific numerical values of x, y
			B(0, 2): $3(0) + 13(2) = 26$		May be implied from identification of (4, 1) or <i>C</i> or from any of
			C(4, 1): 3(4) + 13(1) = 25		these calculations, may be implied from 25 seen with (4, 1) or from
			[A = 52, D = 51, E = 74]		25 indicated in some way as final answer for min value
			Minimum value is 25	A1	25 indicated in some way as final answer for min value (www)
				[2]	
	(iii)		New vertex of feasible region where $2x + y = 11$ and $x + 4y = 8$	M1	Using these two equations simultaneously (or implied)
			$\Rightarrow (5^{-1}, 5^{-1})$	A1	(5.14, 0.71) (x and y values correct as fractions or to at least 2 dp)
			$\binom{7}{7}$		
			$3(5_{7}) + 13(_{7}) = 24_{7}$	A1	24.7 (correct as a fraction or to at least 3sf)
					Fractions may be 'top heavy' i.e. $\frac{36}{7}, \frac{173}{7}$
				[3]	
	(iv)	1	(5, 1) is feasible since $2(5) + 1 = 11$ and $5 + 4(1) = 9 > 8$	B1	Showing that $2x + y < 11$ and $x + 4y > 8$ at (given point) (5. 1)
					Numerical evidence (e.g. 11 and 9) not just ticking as checked
					[Ignore if $-x + 3y < 12$ checked]
			But $3(5) + 13(1) = 28 > 25$ [or 26]	B1	3x + 13y is smaller at (4, 1) [or (0, 2)] than at (5, 1)
					Sight of 28 (or $15 + 13$ or $3(5) + 13$) and one of 25, 26, C or B
					28 and reference to their value from part (ii) or $(4, 1)$ [or $(0, 2)$] oe
					(i.e. the candidate has said that the value is from part (ii))
				[2]	

7	(i)		Suppose that the kiln capacity is k, then each dish uses up $\frac{k}{15}$ and x dishes use up $\frac{kx}{15}$ (and similarly for mugs and pots), so $\frac{kx}{15} + \frac{ky}{50} + \frac{kz}{200} \le k \implies \frac{x}{15} + \frac{y}{50} + \frac{z}{200} \le 1$ so $40x + 12y + 3z \le 600$ a = 40, b = 12, c = 3 and $d = 600$	M1 M1 A1 [3]	Dealing with any of 15, 50 and 200 appropriately (e.g. $x \div 15$ or 15 <i>a</i> , but not 15 <i>x</i>) An inequality of the form $ax + by + cz \le d$, with numerical coefficients and $b = 4c$, but not necessarily integers Coefficients 40, 12, 3, 600 or positive integer multiples of these (stated as <i>a</i> , <i>b</i> , <i>c</i> and <i>d</i> or seen in inequality) $40x + 12y + 3z \le 600$ o.e. (+ integer coefficients) \Rightarrow M1, M1, A1
	(ii)		x	B1 [1]	сао
	(iii)		[z becomes basic and t becomes non-basic]	B1	Correct pivot choice (may be implied from resulting tableau)
	(iv)	(a)	P x y z s t u v RHS 1 0 2 0 0 3 0 -1 68 0 0 1 0 1 2 0 -4 32 0 0 2 1 0 4 0 -3 24 0 0 6 0 0 28 1 -31 368 0 1 0 0 -1 0 1 4	M1 M1 A1 [4] B1	Correct structure with all cells filled in, no blanks 5 different basic columns (0's and a single 1) specifically columns P , x , z (or y) and two of s , t , u RHS values are all non-negative P value in RHS column = 68 [dep on both M marks] Ignore errors in other values provided these conditions are met 36 pots (in context, may imply 0 dishes and 0 mugs)
			Profit £72	B1 [2]	£72, with units
	(iv)	(b)	May not be able to sell all the pots Goods may crack in kiln, damaged goods cannot be sold at full price A particular customer may want a dish or a mug Demand for dishes, mugs, pots not constant	B1 [1]	Any of these or similar Need to explain why making e.g. 0 dishes, 0 mugs, 36 pots may not generate the £72 that it should Not discussing slack variables or changing costs (unless it is to take account of e.g. damaged goods)

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