Oxford Cambridge and RSA

## GCE

## Mathematics

Unit 4736: Decision Mathematics 1
Advanced Subsidiary GCE

## Mark Scheme for June 2017

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

These are the annotations, (including abbreviations), including those used in scoris, which are used when marking

| Annotation in scoris | Meaning |
| :---: | :--- |
| $\checkmark$ and $\mathbf{x}$ |  |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | lgnore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Inderacy mark awarded 0, 1 |
| B0, B1 | Special case mark awarded 0, 1 |
| SC | Omission sign |
| $\wedge$ | Misread |
| MR | Meaning |
| Highlighting | Method mark dependent on a previous mark, indicated by * |
| Other abbreviations in mark scheme | Correct answer only |
| M1 dep* | Or equivalent |
| cao | Rounded or truncated |
| oe | Seen or implied |
| rot | Without wrong working |
| soi |  |
| www |  |

Here are the subject specific instructions for this question paper
Annotations should be used whenever appropriate during your marking.
The $A, M$ and $B$ annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

The following types of marks are available.

## M

A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified

## A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B
Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, $A$ and $B$ marks are given for correct work only - differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

Rules for replaced work
If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.
Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error

MARK SCHEME

| Question |  |  | Answer/Indicative content |  |  |  |  |  |  |  | Mark | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (i) |  | After $1^{\text {st }}$ pass After $2^{\text {nd }}$ pass After $3{ }^{\text {rd }}$ pass After $4^{\text {th }}$ pass After $5^{\text {th }}$ pass | $\begin{array}{r} 10 \\ 3 \\ 3 \\ 3 \\ 3 \end{array}$ | $\begin{aligned} & 3 \\ & 6 \\ & 6 \\ & 4 \\ & 4 \end{aligned}$ | $\begin{array}{r} 6 \\ 10 \\ 4 \\ 5 \\ 5 \end{array}$ | $\begin{array}{r} 12 \\ 4 \\ 5 \\ 6 \\ 6 \end{array}$ | $\begin{array}{r} 4 \\ 5 \\ 10 \\ 10 \\ 10 \end{array}$ | $\begin{array}{r} 5 \\ 12 \\ 12 \\ 12 \\ 12 \end{array}$ | $\begin{aligned} & 12 \\ & 12 \\ & 12 \\ & 12 \\ & 12 \end{aligned}$ | M1 <br> A1 <br> B1 <br> [3] | (Lists may be written vertically) <br> First pass has 12 at right-hand end (even if other values are wrong) (first row or first row after original or identified as pass 1) This list after $3^{\text {rd }}$ pass (even if there were earlier errors) <br> List sorted after $4^{\text {th }}$ pass, $5^{\text {th }}$ pass used to check but no $6^{\text {th }}$ pass |
|  | (ii) | (a) | $\begin{array}{llll} \hline 40 & 27 & 8 & 14 \\ 27 & 40 & 8 & 14 \end{array}$ <br> Note: given list w answers | $14$ | his | may | ppea | befo |  |  | B1 <br> B1 [2] | This list (first or second) <br> This list (first or second) <br> If more than two lists are given, mark the first two only |
|  |  | (b) | 2 |  |  |  |  |  |  |  | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | '2 more' Ignore any passes shown, B 1 is for stating that there are two (more) |


| (i) |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |



| 4 | (i) | $B$ and $E$ |  |  |  |  |  |  | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | Both correct and no others May list vertex orders but need $B$ and $E$ specifically identified |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (ii) | $\begin{array}{ll} A-D-F & =13+16=29 \\ A-E-F & =27+8=35 \end{array}$ <br> Shortest travel time $=29$ minutes |  |  |  |  |  |  | M1 <br> A1 <br> [2] | Evidence of considering both $A-D-F$ and $A-E-F$ or sight of both 35 and 29 or mentioning both $D$ and $E$ 29 , after considering both possibilities <br> SC1 for 29 without showing evidence of considering alternatives |
|  | (iii) | A <br> B <br> 1 0 <br> D <br> E <br> 8 24 <br> 33 24 <br> G <br> 6 20 <br> 20  <br> H <br> 4 18 <br> 18  |  |  |  | $\begin{aligned} & C \\ & \begin{array}{\|l\|l\|} \hline 5 & 19 \\ \hline 19 & \\ \hline & \\ \hline & \\ \hline & 7 \\ \hline & 23 \\ \hline 23 & \\ \hline \end{array} \end{aligned}$ |  |  | M1 M1 dep <br> A1 <br> B1 ft <br> [4] | Correct temporary labels (with no extras) at $A, C$ and $D$ (may imply temporary label at $A$ if permanent label $=6$ but not for $C$ and $D$ ) <br> Some updating of (their) temporary values at $E$ only <br> No penalty for crossing out e.g. 33 provided it is evident that a value has been updated in the lower box for $E$ (and nowhere else, i.e. no updating at $F, G, H$ ) <br> All permanent labels correct (not implied from temporary labels) <br> Order of labelling correct for their permanent labels (using their order gives their permanent labels listed in increasing order) If any permanent label is missing there should be no order label |
|  | (iv) | Total time for direct routes $=222$ then repeat $B$ to $E=24$ Total time $=246$ minutes <br> Repeated arcs $B C$ and $C E$ $C$ is travelled through 4 times |  |  |  |  |  |  | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { [4] } \end{aligned}$ | Attempt at total for half of table i.e. 222 or $444 \div 2$ <br> 246 or 4 hours 6 minutes (cao) [answer 246 o.e. $\Rightarrow$ M1, A1] <br> Accept $B-C-E$ (correct, not ft ) but not e.g. ' $B-E$ via $C$ ' 4 or $3+1=4$ |


| 5 | (i) | $\begin{aligned} & P-J-N-M-L-K-P \\ & \quad 6+5+6+11+12+8=48 \text { miles } \end{aligned}$ | M1 <br> A1 [2] | Route starts $P-J-N-M$ $48$ |
| :---: | :---: | :---: | :---: | :---: |
|  | (ii) | $\begin{array}{ccc} \text { e.g. } P-L-M-N-J-K-P & \text { or } & P-M-N-J-K-L-P \\ & =46 \text { miles } & \\ & =47 \text { miles } \end{array}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & {[2]} \end{aligned}$ | One of these routes, or in reverse Correct length (46 or 47) for their route (having achieved M1) |
|  | (iii) |  | M1 <br> A1 <br> B1 <br> B1 <br> [4] | $J N$ may be written as $N J$, etc. Need not see individual weights At least five of these seven arcs written listed by increasing order of weight, may have $M N$ before $J P$ and/or $M P$ before $K P$ Not just a list of weights and not from diagram Indicating that $K P$ and $M P$ are not chosen <br> Correct tree <br> 33 (miles) |
|  | (iv) | $k>9$ <br> $L M$ must be longer than both $L P$ and $M N$, and the longer of these is $L P=9$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & {[2]} \end{aligned}$ | $k$ greater than $9($ not $k \geq 10$ and not $k \geq 9)$ $L P=9$ and $M N<9$, need to explicitly refer to both $L P$ and $M N$ (i.e. least weight arc at each end of new arc) |
|  | (v) | Shortest closed route that does not use arc $L M$ is $P-M-N-J-K-L-P($ or in reverse $)=47$ miles <br> Shortest route that does use arc $L M$ is $P-L-M-N-J-K-P$ (or in reverse) $=35+k$ miles <br> So $35+k<47 \Rightarrow k<12$ (hence $9<k<12$ ) <br> For reference | M1 <br> M1 <br> A1 <br> [3] | (Shortest route without $L M$ has length) 47 (soi) <br> (Shortest route using $L M$ has length) $35+k$ (soi) <br> $k<12($ not $k \leq 11, \operatorname{not} k=10,11$ and not $k \leq 12)$ [from either M mark] <br> SC1 for $k<12$ (with or without reference to $L K$ ) (or as part of a double inequality, e.g. $9<k<12$ ) if neither M mark has been given |


| 6 | (i) | $\begin{array}{ll} A=(0,4) & B=(0,2) \\ C=(4,1) & D=(4,3) \\ E=(3,5) & \end{array}$ | M1 <br> A1 <br> A1 <br> A1 <br> [4] | Any one coordinate correct $(0,4)$ and $(0,2)$ both correct $(4,1)$ and $(4,3)$ both correct $(3,5)$ correct Ignore not labelling as $A, B, C, D, E$ or mislabelling |
| :---: | :---: | :---: | :---: | :---: |
|  | (ii) | Either checking vertices or using a sliding profit line $\begin{aligned} & B(0,2): 3(0)+13(2)=26 \\ & C(4,1): 3(4)+13(1)=25 \\ & {[\mathrm{~A}=52, \mathrm{D}=51, \mathrm{E}=74]} \end{aligned}$ <br> Minimum value is 25 | M1 <br> A1 <br> [2] | Sight of any $3 x+13 y$ for specific numerical values of $x, y$ May be implied from identification of $(4,1)$ or $C$ or from any of these calculations, may be implied from 25 seen with $(4,1)$ or from 25 indicated in some way as final answer for min value <br> 25 indicated in some way as final answer for min value (www) |
|  | (iii) | New vertex of feasible region where $2 x+y=11$ and $x+4 y=8$ $\begin{aligned} & \Rightarrow\left(5 \frac{1}{7}, \frac{5}{7}\right) \\ & 3\left(5 \frac{1}{7}\right)+13\left(\frac{5}{7}\right)=24 \frac{5}{7} \end{aligned}$ | M1 <br> A1 <br> A1 <br> [3] | Using these two equations simultaneously (or implied) $(5.14,0.71)$ ( $x$ and $y$ values correct as fractions or to at least 2 dp ) <br> 24.7 (correct as a fraction or to at least 3sf) <br> Fractions may be 'top heavy' i.e. $\frac{36}{7}, \frac{173}{7}$ |
|  | (iv) | $(5,1)$ is feasible since $2(5)+1=11$ and $5+4(1)=9>8$ <br> But $3(5)+13(1)=28>25$ [or 26$]$ | B1 <br> B1 <br> [2] | Showing that $2 x+y \leq 11$ and $x+4 y \geq 8$ at (given point) $(5,1)$ Numerical evidence (e.g. 11 and 9) not just ticking as checked [Ignore if $-x+3 y \leq 12$ checked] <br> $3 x+13 y$ is smaller at $(4,1)[$ or $(0,2)]$ than at $(5,1)$ <br> Sight of 28 (or $15+13$ or $3(5)+13$ ) and one of $25,26, C$ or $B$ 28 and reference to their value from part (ii) or $(4,1)$ [or $(0,2)]$ oe (i.e. the candidate has said that the value is from part (ii)) |



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