



Oxford Cambridge and RSA

Level 3 Cambridge Technical in Engineering

05822/05823/05824/05825/05873

Formula Booklet

Unit 1 Mathematics for engineering

Unit 2 Science for engineering

Unit 3 Principles of mechanical engineering

Unit 4 Principles of electrical and electronic engineering

Unit 23 Applied mathematics for engineering

This booklet contains formulae which learners studying the above units and taking associated examination papers may need to access.

Other relevant formulae may be provided in some questions within examination papers. However, in most cases suitable formulae will need to be selected and applied by the learner. Clean copies of this booklet will be supplied alongside examination papers to be used for reference during examinations.

Formulae have been organised by topic rather than by unit as some may be suitable for use in more than one unit or context.

Note for teachers

This booklet does not replace the taught content in the unit specifications or contain an exhaustive list of required formulae. You should ensure all unit content is taught before learners take associated examinations.

1. Trigonometry and Geometry

1.1 Geometry of 2D and 3D shapes

1.1.1. Circles and arcs

Circle: radius r

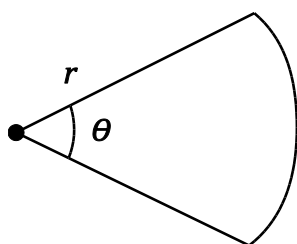
$$\text{Area of a circle} = \pi r^2$$

$$\text{Circumference of a circle} = 2\pi r$$

Co-ordinate equation of a circle: radius r , centre (a, b)

$$(x - a)^2 + (y - b)^2 = r^2$$

Arc and sector: radius r , angle θ



Arc length = θr , for θ expressed in radians

Area of sector = $\frac{1}{2}r^2\theta$, for θ expressed in radians

Arc length = $\frac{\theta}{180}\pi r$, for θ expressed in degrees

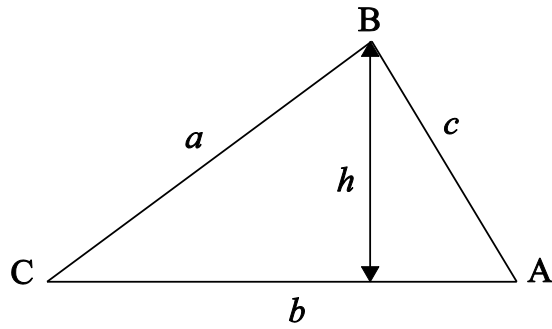
Area of sector = $\frac{\theta}{360}\pi r^2$, for θ expressed in degrees

Converting between radians and degrees

$$x \text{ radians} = \frac{180x}{\pi} \text{ degrees}$$

$$x \text{ degrees} = \frac{\pi x}{180} \text{ radians}$$

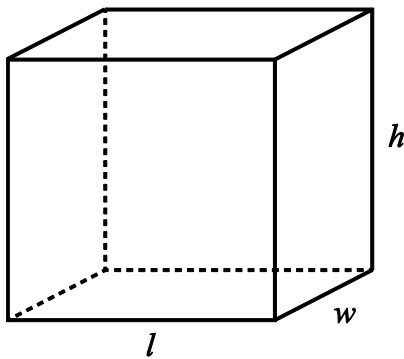
1.1.2 Triangles



$$\text{Area} = \frac{1}{2}bh \text{ or } \frac{1}{2}bc \sin A$$

1.2 Volume and Surface area of 3D shapes

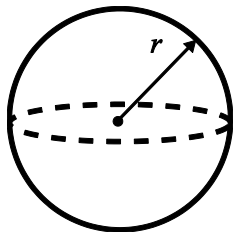
Cuboid



$$\begin{aligned} \text{Surface area} &= 2lw + 2wh + 2hl \\ &= 2(lw + wh + hl) \end{aligned}$$

$$\text{Volume} = lwh$$

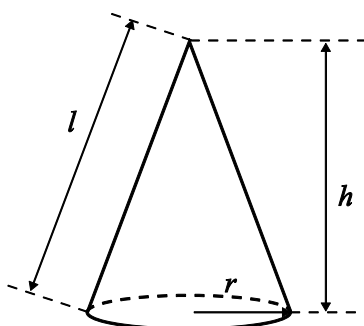
Sphere



$$\text{Surface area} = 4\pi r^2$$

$$\text{Volume} = \frac{4}{3}\pi r^3$$

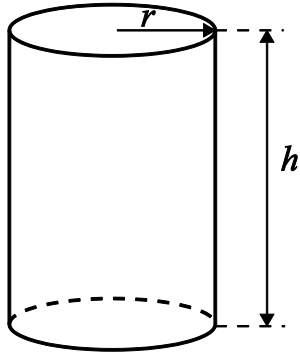
Cone



$$\text{Surface area} = \pi r^2 + \pi rl$$

$$\text{Volume} = \frac{1}{3}\pi r^2 h$$

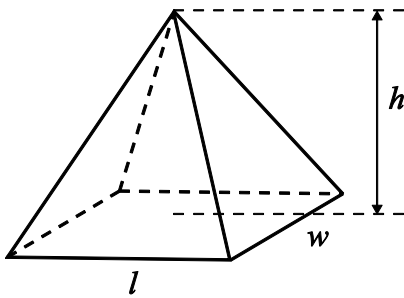
Cylinder



$$\text{Surface area} = 2\pi r^2 + 2\pi r h$$

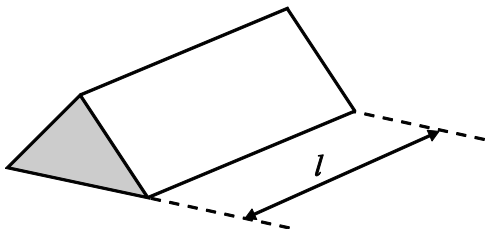
$$\text{Volume} = \pi r^2 h$$

Rectangular Pyramid



$$\text{Volume} = \frac{lwh}{3}$$

Prism

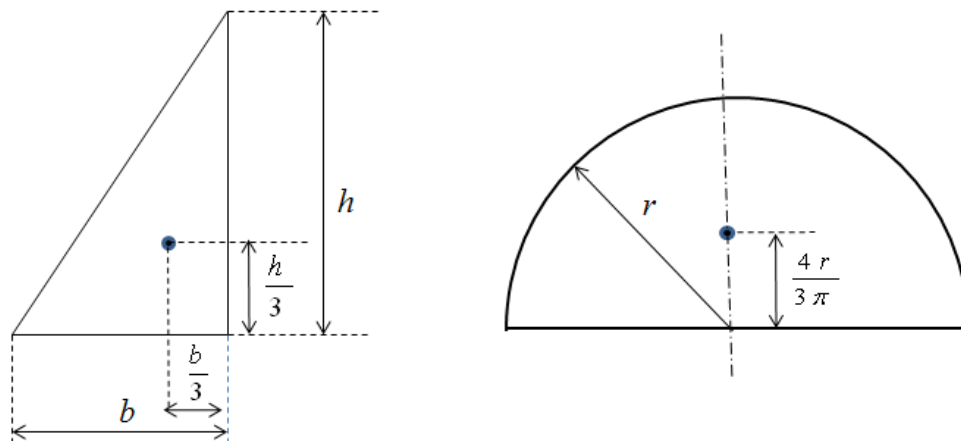


$$\text{Volume} = \text{area of shaded cross-section} \times l$$

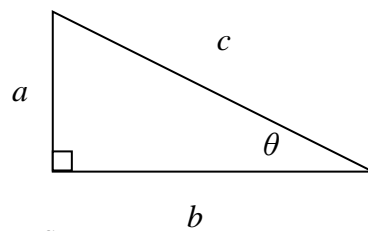
Density

$$\text{Density} = \frac{\text{mass}}{\text{volume}}$$

1.3 Centroids of planar shapes



1.4 Trigonometry

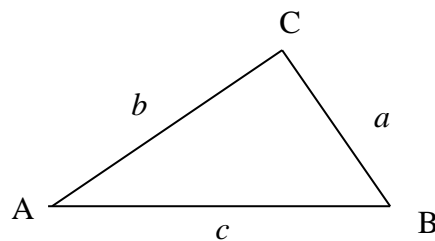


$$\sin \theta = \frac{a}{c}$$

$$\cos \theta = \frac{b}{c}$$

$$\tan \theta = \frac{a}{b}$$

Pythagoras' rule: $c^2 = a^2 + b^2$



Sine rule: $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule: $a^2 = b^2 + c^2 - 2bc \cos A$

1.4.1 Trigonometric identities

Basic trigonometric values

$$\sin 60^\circ = \frac{\sqrt{3}}{2}$$

$$\cos 60^\circ = \frac{1}{2}$$

$$\tan 60^\circ = \sqrt{3}$$

$$\sin 45^\circ = \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\tan 45^\circ = 1$$

$$\sin 30^\circ = \frac{1}{2}$$

$$\cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\tan 30^\circ = \frac{1}{\sqrt{3}}$$

Trigonometric identities

$$\sin A = \cos(90^\circ - A) \text{ for angle } A \text{ in degrees}$$

$$\cos A = \sin(90^\circ - A) \text{ for angle } A \text{ in degrees}$$

$$\sin A = \cos\left(A - \frac{\pi}{2}\right)$$

$$\cos A = -\sin\left(A - \frac{\pi}{2}\right)$$

$$\tan A = \frac{\sin A}{\cos A}$$

$$\sin^2 A + \cos^2 A = 1$$

$$\sin(-A) = -\sin A$$

$$\cos(-A) = \cos A$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A$$

2. Calculus

2.1 Differentiation

$f(x)$	$\frac{df(x)}{dx}$
c	0
x^n	nx^{n-1}
$\sin(ax)$	$a \cos(ax)$
$\cos(ax)$	$-a \sin(ax)$
$\tan(ax)$	$a \sec^2(ax)$
e^{ax}	ae^{ax}
$\ln(ax)$	$\frac{1}{x}$
a^x	$a^x \ln a$
$\log_a x$	$\frac{1}{x \ln a}$

2.1.1 Differentiation of the product of two functions

$$\text{If } y = u \times v \quad \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

2.1.2 Differentiation of the quotient of two functions

$$\text{If } y = \frac{u}{v} \quad \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

2.1.3 Differentiation of a function of a function

$$\text{If } y = u(v) \quad \frac{dy}{dx} = \frac{du}{dv} \frac{dv}{dx}$$

2.2 Integration

2.2.1 Indefinite integrals

$f(x)$	$\int f(x) dx (+c)$
a	ax
x^n for $n \neq -1$	$\frac{x^{n+1}}{n+1}$
$\frac{1}{x}$	$\ln x $
e^{ax}	$\frac{e^{ax}}{a}$
a^x	$\frac{a^x}{\ln a}$
$\sin(ax)$	$\frac{-\cos(ax)}{a}$
$\cos(ax)$	$\frac{\sin(ax)}{a}$

2.2.2 Definite integral

$$\int_a^b f(x) dx = [F(x)]_a^b = F(b) - F(a)$$

2.2.3 Integration by parts

$$\int u \frac{dv}{dx} dx = uv - \int v \frac{du}{dx} dx$$

3. Algebraic formulae

3.1 Solution of quadratic equation

$$ax^2 + bx + c = 0, \quad a \neq 0$$

$$\Rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

3.2 Exponentials/Logarithms

$$y = e^{ax} \Rightarrow \ln y = ax$$

4. Measurement

Absolute error = indicated value – true value

Relative error = $\frac{\text{absolute error}}{\text{true value}}$

Absolute correction = true value – indicated value

Relative correction = $\frac{\text{absolute correction}}{\text{true value}}$

5. Statistics

For a sample, size N , $x_1, x_2, x_3, \dots, x_N$,

sample mean $\bar{x} = \frac{x_1 + x_2 + x_3 + \dots + x_N}{N}$

standard deviation $S = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - \bar{x})^2} = \sqrt{\frac{1}{N} \sum_{i=1}^N x_i^2 - (\bar{x})^2}$

5.1 Probability

For events A and B , with probabilities of occurrence $P(A)$ and $P(B)$,

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

If A and B are mutually exclusive events,

$$P(A \text{ and } B) = 0$$

$$P(A \text{ or } B) = P(A) + P(B)$$

If A and B are independent events,

$$P(A \text{ and } B) = P(A) \times P(B)$$

6. Mechanical equations

6.1 Stress and strain equations

$$\text{axial stress } (\sigma) = \frac{\text{axial force}}{\text{cross sectional area}}$$

$$\text{axial strain } (\zeta) = \frac{\text{change in length}}{\text{original length}}$$

$$\text{shear stress } (\tau) = \frac{\text{shear force}}{\text{shear area}}$$

$$\text{Young's modulus } (E) = \frac{\text{stress}}{\text{strain}}$$

$$\text{Working or allowable stress} = \frac{\text{ultimate stress}}{\text{Factor of Safety (FOS)}}$$

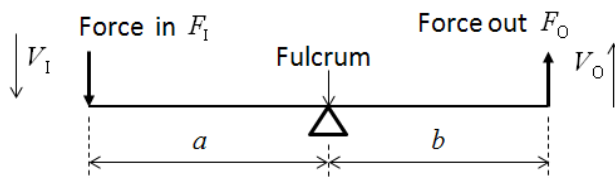
6.2 Mechanisms

$$\text{Mechanical advantage (MA)} = \frac{\text{output force (or torque)}}{\text{input force (or torque)}}$$

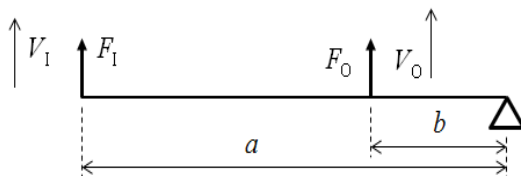
$$\text{Velocity ratio (VR)} = \frac{\text{velocity of output from a mechanism}}{\text{velocity of input to a mechanism}}$$

6.2.1 Levers

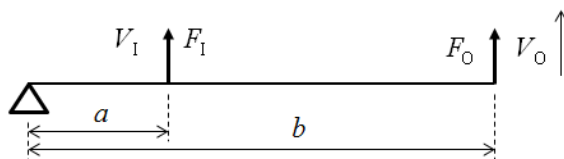
- Class one lever



- Class two lever



- Class three lever



$$MA = \frac{F_0}{F_1} = \frac{a}{b}$$

$$VR = \frac{V_0}{V_1} = \frac{b}{a}$$

6.2.2 Gear systems

$$\text{MA} = \frac{\text{Number of teeth on output gear}}{\text{Number of teeth on input gear}}$$

$$\text{VR} = \frac{\text{Number of teeth on input gear}}{\text{Number of teeth on output gear}}$$

6.2.3 Belt and pulley systems

$$\text{MA} = \frac{\text{Diameter of output pulley}}{\text{Diameter of input pulley}}$$

$$\text{VR} = \frac{\text{Diameter of input pulley}}{\text{Diameter of output pulley}}$$

6.3 Dynamics

Newton's equation force = mass x acceleration ($F = ma$)

Gravitational potential energy (W_p) = mass x gravitational acceleration x height (mgh)

Kinetic energy (W_k) = $\frac{1}{2}$ mass x velocity² ($\frac{1}{2}mv^2$)

Work done = force x distance (Fs)

Instantaneous power = force x velocity (Fv)

Average power = work done / time ($\frac{W}{t}$)

Friction Force \leq coefficient of friction x normal contact force ($F \leq \mu N$)

Momentum of a body = mass x velocity (mv)

Pressure = force / area ($\frac{F}{A}$)

6.4 Kinematics

Constant acceleration formulae

a – acceleration

s – distance

t – time

u – initial velocity

v – final velocity

$v^2 = u^2 + 2as$
$s = ut + \frac{1}{2}at^2$
$v = u + at$
$s = \frac{1}{2}(u + v)t$
$s = vt - \frac{1}{2}at^2$

6.5 Fluid mechanics

Pressure due to a column of liquid

= height of column \times gravitational acceleration \times density of liquid ($hg\rho$)

Up-thrust force on a submerged body

= volume of submerged body \times gravitational acceleration \times density of liquid ($Vg\rho$)

6.5.1 Energy equations

Non-flow energy equation

$$U_1 + Q = U_2 + W \quad \text{so } Q = (U_2 - U_1) + W$$

where Q = energy entering the system

W = energy leaving the system

U_1 = initial energy in the system

U_2 = final energy in the system.

Steady flow energy equation

$$Q = (W_2 - W_1) + W$$

where Q = heat energy supplied to the system

W_1 = energy entering the system

W_2 = energy leaving the system

W = work done by the system.

7. Thermal Physics

p – pressure

V – volume

C – constant

T – absolute temperature

n – number of moles of a gas

R – the gas constant

Boyle's law $pV = C$ $p_1V_1 = p_2V_2$

Charles' law $\frac{V}{T} = C$ $\frac{V_1}{T_1} = \frac{V_2}{T_2}$

Pressure law $\frac{p}{T} = C$ $\frac{p_1}{T_1} = \frac{p_2}{T_2}$

Combined gas law $\frac{p_1V_1}{T_1} = \frac{p_2V_2}{T_2}$

Ideal gas law $pV = nRT$

Characteristic gas law $pV = mRT$ where m = mass of specific gas and
 R = specific gas constant

Efficiency $\eta = \frac{\text{work output}}{\text{work input}}$

7.1 Heat formulae

Latent heat formula

Heat absorbed or emitted during a change of state, $Q = mL$

where Q = Energy, L = latent heat of transformation, m = mass

Sensible heat formula

Heat energy, $Q = mc\Delta T$

where Q = Energy, m = mass, c = specific heat capacity of substance,
 ΔT is change in temperature

8. Electrical equations

Q = charge V = voltage I = current R = resistance ρ = resistivity P = power E = electric field strength (capacitors) C = capacitance L = inductance t = time l = length τ = time constant W = energy A = cross sectional area Φ = magnetic flux	N = number of turns Θ = angle (in radians) f = Frequency (in cycles per second) $\omega = 2\pi f$ X_L, X_C = inductive reactance, capacitive reactance Z = impedance ϕ = phase angle E = emf (motors) I_a = armature current I_f = field current I_l = load current R_a = armature resistance R_f = field resistance n = speed (motors) T = torque η = efficiency
--	---

Charge and potential energy	$Q = It$ $V = W/Q$ $W = Pt$
Drift velocity (current)	$I = nAve$
Power	$P = VI$ $P = I^2R$ $P = V^2/R$
Resistance and Ohms law	Series resistance: $R = R_1 + R_2 + R_3 + \dots$ Parallel resistance: $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$ Ohms law: $R = V/I$ $V = IR$ $I = V/R$
Resistivity	$\rho = RA/l$
Electric field and capacitance	$E = V/d$ $C = Q/V$ $W = \frac{1}{2}QV$
Inductance and self-inductance	$L = \Phi N / I$ $W_L = \frac{1}{2}LI^2$
RC circuits	$\tau = RC$ $v = v_0 e^{-t/RC}$
AC waveforms	$v = V \sin \Theta$ $i = I \sin \Theta$ $v = V \sin \omega t$ $i = I \sin \omega t$
AC circuits – resistance and reactance	$R = V/I$ $X_L = V/I$ and $X_L = 2\pi fL$ $X_C = V/I$ and $X_C = \frac{1}{2\pi fC}$
Series RL and RC circuits	$Z = \sqrt{(R^2 + X_L^2)}$ and $\cos \phi = R/Z$ $Z = \sqrt{(R^2 + X_C^2)}$ and $\cos \phi = R/Z$

Series RLC circuits	<p>When $X_L > X_C$ $Z = \sqrt{R^2 + (X_L - X_C)^2}$ and $\cos\phi = R/Z$ When $X_C > X_L$ $Z = \sqrt{R^2 + (X_C - X_L)^2}$ and $\cos\phi = R/Z$ When $X_L = X_C$ $Z = R$</p>
DC motor	$V = E + I_a R_a$
DC generator	$V = E - I_a R_a$
DC Series wound self-excited generator	$V = E - I_a R_t$ Where $R_t = R_a + R_f$
DC Shunt wound self-excited generator	$V = E - I_a R_a$ Where $I_a = I_f + I_l$ $I_f = V/R_f$ $I_l = P/V$
DC Series wound motor	$V = E + I_a R_t$ Where $R_t = R_a + R_f$ $E \propto \Phi n$
DC Shunt wound motor - No-load conditions:	$V = E_1 + I_a R_a$ Where $I_a = I_l - I_f$ $I_f = V/R_f$
DC Shunt wound motor - Full load conditions:	$V = E_2 + I_a R_a$ Where $I_a = I_l - I_f$ $E_1/E_2 = n_1/n_2$ $T_1/T_2 = (\Phi_1 I_{a1})/(\Phi_2 I_{a2})$
Speed control of DC motors - Shunt motor	$V = E + I_a R_a$ $n = (V - I_a R_a)/(k\Phi)$
DC Machine efficiency	$\eta = \text{output/input}$ $\eta_l = 1 - (\text{losses/input})$

Copyright Information:

OCR is committed to seeking permission to reproduce all third-party content that it uses in its assessment materials. OCR has attempted to identify and contact all copyright holders whose work is used in this paper. To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced in the OCR Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download from our public website (www.ocr.org.uk) after the live examination series.

If OCR has unwittingly failed to correctly acknowledge or clear any third-party content in this assessment material OCR will be happy to correct its mistake at the earliest possible opportunity.

For queries or further information please contact the Copyright Team, First Floor, 9 Hills Road, Cambridge CB2 1GE.

OCR is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.