

GCE

Mathematics A

Unit H240/03: Pure Mathematics and Mechanics

Advanced GCE

Mark Scheme for June 2018

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Annotations and abbreviations

Annotation in scoris	Meaning
✓and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
۸	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark	Meaning
Other abbreviations in mark scheme	Meaning
Other abbreviations in mark scheme E1	Meaning Mark for explaining a result or establishing a given result
Other abbreviations in mark scheme E1 dep*	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by *
Other abbreviations in mark scheme E1 dep* cao	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only
Other abbreviations in mark scheme E1 dep* cao oe	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent
Other abbreviations in mark scheme E1 dep* cao oe rot	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated
Other abbreviations in mark scheme E1 dep* cao oe rot soi	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied
Other abbreviations in mark schemeE1dep*caooerotsoiwww	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working
Other abbreviations in mark schemeE1dep*caooerotsoiwwwAG	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working Answer given
Other abbreviations in mark schemeE1dep*caooerotsoiwwwAGawrt	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working Answer given Anything which rounds to
Other abbreviations in mark scheme E1 dep* cao oe rot soi www AG awrt BC	Meaning Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working Answer given Anything which rounds to By Calculator

Subject-specific Marking Instructions for A Level Mathematics A

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Ε

Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

Mark Scheme

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

Mark Scheme

i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j If in any case the scheme operates with considerable unfairness consult your Team Leader.

(Juestio	n	Answer	Marks	AO		Guidance	
1	(i)		$(x+4)^2 - 16 + (y-1)^2 - 1 - 7 = 0$	M1	1.1	Ε	Correct method to find centre of circle	e.g. $(x\pm 4)^2$ and
			$(x+4)^{2} + (y-1)^{2} = 24$					$(y\pm 1)^2$ seen (or
								implied)
			<i>C</i> (-4,1)	A1	1.1	Е		I ····
				[2]				
1	(ii)		Radius = $\sqrt{24}$	B1	1.1	Е	oe e.g. $2\sqrt{6}$	
				[1]				
2			Attempt process for finding both values	M1	1.1 a	E	e.g. squaring both sides to obtain 3	Or consider two
							terms on both sides	linear equations
							$(4x^2 - 4x + 1 = x^2 + 6x + 9)$	$(2x-1) = \pm (x+3)$
			$3x^2 - 10x - 8 = 0$	A1	1.1	Е		1 correct solution
						_		for A1
			Obtain 4 and $-\frac{2}{-}$	Al	1.1	E	BC	SC one correct
			3					solution from one
				[3]				inical equation B1
3			DR					
			$x + 3 \ge 14.5$	M1	3.1 b	Е	Accept any inequality or equals and	
				4.1	11	Б	any letter for the width	M1A1 composi
			$x \ge 11.5$	AI	1.1	E	Correct inequality (seen or implied)	answer with no
								working
			x(x+3) < 180	M1	3.1 b	Е	Accept any inequality or equals	C
			$x^{2} + 3x - 180(<0) \Rightarrow (x - 12)(x + 15)(<0)$	M1	1.1	Е	Correct expansion and attempt to solve	SC B1: $x < \sqrt{60}$
							three term quadratic	~ ~
			-15 < x < 12	A1	1.1	C	Correct inequalities (seen or implied)	B1: $x \ge 29/6$
			$11.5 \le x < 12$	B1	1.1	C		
				נסן				

(Juestio	n	Answer	Marks	AO		Guidance	
4	(i)	(a)	$fg(x) = f(x^2+2) = (x^2+2)^3$	B 1	1.1	Е		
				[1]				
4	(*)	(h)	2	D1	11	Б	No simulification required	
4	(1)	(D)	$gf(x) = g(x^3) = (x^3)^2 + 2(=x^6 + 2)$	D1	1.1	E	No simplification required	
				[1]				
4	(ii)		DR					
			$(x^{2}+2)^{3} = (x^{2})^{3} + 3(x^{2})^{2}(2) + 3(x^{2})(2)^{2} + 2^{3}$	M1	1.1	E	Binomial expansion of their $(x^2 + 2)^3$	Allow one slip
							- correct powers and coefficients	
			$fg(x) = x^6 + 6x^4 + 12x^2 + 8$	A1	1.1	С	confect powers and coefficients	
			$f_{g}(x) - gf(x) - 24 \rightarrow 6x^{4} + 12x^{2} - 18 = 0$	A1	2.1	С		
			$(1)^{-1}g(x) - g(x) - 24 \rightarrow 0x + 12x - 10 = 0$	M1	11	C	Correct method for solving their	If MO next two
			$x^{+} + 2x^{2} - 3 = 0 \Longrightarrow (x^{2} - 1)(x^{2} + 3) = 0$	1411	1,1	C	quadratic in x^2	marks become B marks
			$x^{2} + 3 = 0$ has no real solutions	A1	2.4	А	$x^2 + 3 \neq 0$ is acceptable for this mark	
			$x^2 - 1 = 0 \Longrightarrow x = \pm 1$	A1	2.2a	Α	1 I	
				[6]				
5	(i)		h = 2	B1	1.1	E		
			$\frac{h\left[1+\frac{1}{2}+\frac{1}{2}+2\left(-\frac{1}{2}\right)\right]}{2}$	M1	2.1	E	Use of correct formula with correct	Condone one error
			$2\left\lfloor 2 + 4 + 2\left(2 + \sqrt{2}\right) \right\rfloor$				(exact) y-values with their n	in values
			$I \approx \frac{3}{2} + \frac{2}{2}$	A1	1.1	С		
			$4^{-2} + \sqrt{2}$					
			1 $(2-\sqrt{2})$ $2-\sqrt{2}$	M1	3.1 a	Е	Correct method for rationalising the	
			$\frac{1}{2+\sqrt{2}} = \frac{1}{(2+\sqrt{2})(2-\sqrt{2})} = \frac{1}{2}$				correct simplification	
			$I \sim \frac{3}{2} + (2 - \sqrt{2}) - \frac{11}{2} - \sqrt{2}$	A1	2.2a	А	$\mathbf{A}\mathbf{G}$ – at least one step of intermediate	Must be convincing
			$4^{-1}(2^{-1}\sqrt{2}) - \frac{1}{4}$ $\sqrt{2}$	[5]			working (from application of trapezium rule to given result)	as AG

	Questic	n	Answer	Marks	AO		Guidance	
5	(ii)		$x = u^2 \Longrightarrow dx = 2u du$	M1*	3.1 a	E	An attempt at integration by sub -	Limits not required
							allow any genuine attempt (as a	for first four marks
							minimum must differentiate their sub.	
							and remove all <i>x</i> 's)	
			$\int_{-1}^{4} dx \int_{-1}^{2} 2u$	A1	1.1	С	Correct integral in terms of <i>u</i>	
			$\int_{0} \frac{1}{2 + \sqrt{x}} = \int_{0} \frac{1}{2 + u} du$					
			$2 + \sqrt{3} = 2 + \sqrt{3}$	Den*M1	21	С	Re-writes integral in the form	Or use $t - 2 + u$ to
			$=2\int_{0}^{2}\frac{2+u-2}{2}du=2\int_{0}^{2}1-\frac{2}{2}du$	Dep MI	2.1	C	• h	obtain integral of
			50 2+u 50 2+u				$\int a + \frac{b}{1} du$	botani integral or
							J = 1+u	the form $\int a + \frac{b}{-} dt$
								J t
			$=2\left[u-2\ln(2+u)\right]_{0}^{2}$	Alft	1.1	А	Correctly integrates their $\int a + \frac{b}{-} du$	$\int 2 - \frac{4}{-} dt$
							J = J = J = J = J = J = J = J = J = J =	J t
								$= 2t - 4\ln t$
			$= 2 \{ (2 - 2\ln(2 + 2)) - (0 - 2\ln(2 + 0)) \}$	M1	1.1	C	Uses correct limits correctly	
							(dependent on both previous M marks)	
			$=2(2-2\ln 2)$	A1	2.2a	A	oe e.g. $4 - 4 \ln 4 + 4 \ln 2$	
				[6]				
5	(iii)		11 - 5 - 2(2 - 21 - 2)	M1	1.1a	С	Setting the given result approx. equal	
			$\frac{\sqrt{2}}{4} \approx 2(2-2\ln 2)$				to their (ii)	
			$1 = 2 = 5 + \sqrt{2}$	A1	2.2a	Α	$k = \frac{5}{2}$	
			$\ln 2 \approx \frac{1}{16} + \frac{1}{4}$	[2]			$\kappa = 16$	
				r_1				
	1							

(Juesti o	on	Answer	Marks	AO		Guidance	
6	(i)		$\sin\left(2\theta + \frac{\pi}{4}\right) = 3\cos\left(2\theta + \frac{\pi}{4}\right)$ $\sin 2\theta \cos \frac{\pi}{4} + \sin \frac{\pi}{4}\cos 2\theta = 3\cos 2\theta \cos \frac{\pi}{4} - 3\sin 2\theta \sin \frac{\pi}{4}$	M1	1.1	Е	Correct use of compound angle formulae at least once	
			$4\sin 2\theta = 2\cos 2\theta$ $2\frac{\sin 2\theta}{\cos 2\theta} = 1 \Longrightarrow \tan 2\theta = \frac{1}{2}$	A1 A1	1.1 2.2a	E E	Not from incorrect working AG – at least one step of intermediate working seen	
				[3]				
			ALT: $\tan\left(2\theta + \frac{\pi}{4}\right) = 3$	B1				
			$\frac{\tan 2\theta + 1}{1 - \tan 2\theta} = 3 \implies \tan 2\theta + 1 = 3(1 - \tan 2\theta)$	M1			Correct use of compound angle formula for tan and removal of fraction	
			$\tan 2\theta = \frac{1}{2}$	A1				
6	(ii)		$\tan 2\theta = \frac{1}{2} \Longrightarrow \frac{2\tan\theta}{1-\tan^2\theta} = \frac{1}{2}$	M1*	3.1a	Е	Double angle formula for $\tan 2\theta$	Allow one sign slip in formula
			$\tan^2\theta + 4\tan\theta - 1 = 0$	Dep*M1	1.1	Е	Rearranges correctly to form 3-term quadratic in tan	
			$\tan\theta = -2\pm\sqrt{5}$	A1	1.1	С	BC - One correct exact value	
			$-2 + \sqrt{5} > 0$ so $\tan \theta = -2 + \sqrt{5}$ gives acute angle	A1	2.3	А	Explicit rejection and reason for rejection	
			$\therefore \tan \theta = -2 - \sqrt{5}$	A1	2.2a	Α	This value only	
				[5]				

Question	Answer	Marks	AO		Guidance	
7	$(2x-1)^{3} \frac{dy}{dx} + 4y^{2} = 0$ $-\frac{1}{4} \int \frac{dy}{y^{2}} = \int \frac{dx}{(2x-1)^{3}}$	M1	2.5	E	Attempt to separate variables	
	$\int \frac{\mathrm{d}y}{v^2} = -\frac{1}{v}$	A1	1.1	Е		
	$\int \frac{\mathrm{d}x}{(2x-1)^3} = \frac{(2x-1)^{-2}}{(2)(-2)}$	M1 A1	1.1 1.1	E C	M1 for $k(2x-1)^{-2}$	
	$\frac{1}{4y} = -\frac{1}{4(2x-1)^2} + c, \ (1,1) \Longrightarrow c = \dots$	M1	2.1	C	Use of $(1, 1)$ to find c – dependent on the previous two M marks and substituted into correct form	
	$\frac{1}{y} = -\frac{1}{(2x-1)^2} + 2$	A1	2.2a	А	Oe	
	$\frac{1}{y} = \frac{2(2x-1)^2 - 1}{(2x-1)^2}$	M1	3.1 a	A	Correct method for combining both terms on rhs (dependent on previous M mark) before taking the reciprocal	Or re-write in terms of <i>y</i>
	$y = \frac{(2x-1)^2}{2(2x-1)^2 - 1}$	M1	1.1	Α	Taking the reciprocal (dependent on previous M marks) and making y the subject	Remove triple- decker fractions
	$y = \frac{4x^2 - 4x + 1}{8x^2 - 8x + 1}$	A1	2.2a	А	a = 4, b = 8	
		[9]				

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(Question	Answer	Marks	AO		Guidance
8	(i)	$\mathbf{g} = \begin{pmatrix} 0\\ -9.8 \end{pmatrix}$	B1	1.2	E	
		$ \begin{pmatrix} 15\\-8 \end{pmatrix} + \begin{pmatrix} -7\\-2 \end{pmatrix} + 5 \begin{pmatrix} 0\\-9.8 \end{pmatrix} = 5\mathbf{a} $	M1	3.3	E	Use of $\mathbf{F} = m\mathbf{a}$ with correct <i>m</i> and two terms of \mathbf{F} correct
		$\mathbf{a} = \begin{pmatrix} 1.6 \\ -11.8 \end{pmatrix} \text{ or } \begin{pmatrix} 1.6 \\ -g-2 \end{pmatrix}$	A1 [3]	3.4	C	
8	(ii)	$\mathbf{s} = \frac{1}{2} \begin{pmatrix} 1.6 \\ -11.8 \end{pmatrix} (10)^2$	M1	3.4	E	Use of $\mathbf{s} = \mathbf{u}t + \frac{1}{2}\mathbf{a}t^2$ with $t = 10$
		$\mathbf{s} = \begin{pmatrix} 80\\ -590 \end{pmatrix}$	A1ft	1.1	Е	50 a
		Position vector is $\begin{pmatrix} 82\\ -545 \end{pmatrix}$	A1	1.1	С	
			[3]			
9	(i)	25 N	B1 [1]	3.4	E	
9	(ii)		M1	3.3	E	eg moments about A – correct number of terms
		2(100) = 75x + (x + 0.5)(25)	A1ft	1.1	С	Follow through their 25 only
		x=1.875	A1 [3]	1.1	С	
9	(iii)		M1	3.3	Е	moments about D – correct number of terms – oe (leading to an equation in W)
		(x+0.5-2)(100) = W(4-0.5-x)	A1ft	1.1	С	Follow through their <i>x</i> only
		$W = 23.1 \mathrm{N}$	A1 [3]	1.1	A	Accept 23 or better 23.076923

()uestio	on	Answer	Marks	AO		Guidance	
9	(iv)	(a)	Modelling the stone as a particle assumes that the					
			weight of the stone block acts exactly at <i>B</i> therefore					
			the block's dimensions (or the distribution of the	Di				
			mass of the block) have not been taken into	B1	3.5 b	A	Accept 'uniform'	
			consideration					
				[1]				
9	(iv)	(b)	Modelling the plank as a rigid rod assumes that the	B1	3.5b	Α		
			plank remains in a straight line and does not bend					
				[1]				
10	(i)		$4\sin 2\theta = 6\sin \theta$	B1	3.3	E	Resolving horizontally	
				M1	3.1a	E	Use of double angle formulae	
			$8\sin\theta\cos\theta = 6\sin\theta$	A1	1.1	E		
				A1	2.2a	С	AG	41.409622
			$\cos\theta = - \Rightarrow \theta = 41.4^{\circ}$					
			•	[4]				
10	(ii)		$P = 4\cos 2\theta + 6\cos \theta$	M1	3.3	Е	Resolving vertically – allow sin/cos	
10	(11)				0.0	-	errors	
			P=5	Δ1	11	F	Accept 5 002 or better	
			1-5	[2]	1.1	Ľ	recept 5.002 of better	
10	(iiii)	(a)	$3\sin\theta$ and $P-3\cos\theta$	 	11	E	Resolving horizontally and vertically	Alt – M1 for cosine
10	(111)	(u)		DI	1.1		Tressiving nonzontary and verticary	rule with their P 3
								and 41.4 A1 for
								11 4966 or 115
				M1	11	F	Pythagoras on two forces – both must	11.1900 01 11.5
			$\sqrt{(3\sin\theta)^2 + (P - 3\cos\theta)^2}$		1.1	Г	include A1 A	
			Magnitude is 3 30 N	A 1	2.20	C	3 1 or better	3 30116/10
			Wagintude 15 5.571		2.2a	C	5.4 01 better	5.5711047
				[3]				
1		1				1		

(QuestionAnswerMarksAOGuidance							
10	(iii)	(b)	$P-3\cos\theta$	M1	3.1 a	E	Where α is the angle below the	Alt - M1 for
			$\tan \alpha = \frac{3\sin \theta}{3\sin \theta}$				horizontal	$\sin \alpha \sin 41.4$
			54.2° below the horizontal	A1	3.2a	Α	54.2 or better – must indicate 'below	54.18696
							horizontal' or equivalent to the	
							'downward vertical' (35.8) – direction	
							may be shown on diagram with	
							minimum of arrow on resultant or	
				[2]			arrows on both components	
11	(i)		a = k + 0.06t	[<u></u>] 	11	F		
-	(1)		k + 0.06(20) = 1.3	M1	1.1	E	Use of $t = 20$ and $a = 1.3$ in their a	
			k = 1.3 - 1.2 = 0.1	A1	1.1	E		
				[3]				
11	(ii)			M1*	3.1a	Е	Attempt to integrate – all powers	
							increased by 1 (but not just multiplying	
						_	by t)	
			$s = 0.05t^2 + 0.01t^3(+c)$	A1ft	1.1	E	$s = \frac{1}{kt^2} + 0.01t^3$	
							2	
			$t = 0, s = 0 \Longrightarrow c = 0$	B1	2.1	Α	From a correct expression for <i>s</i>	If $c = 0$ stated then
				D164	11	Б	12 + 204	must give a reason
			t = 20, v = 14	BIII	1.1	E	12+20k	
			$s_1 = 0.05(20)^2 + 0.01(20)^3$	dep*M1	3.4	С	Finding distance travelled after 20s	
							(for reference $s_1 = 100$)	
			$25^2 = 14^2 + 2(1.3)s_2$	MI	3.3	A	Use of $v^2 = u^2 + 2as$ with $v = 25$ and	
							a = 1.3 and their u	
			Total distance $= s_1 + s_2 = 265 \text{ m}$	Al	2.2a	A	All previous marks must have been	
				[7]			awarded	
				[/]				

Q)uesti o	n	Answer	Marks	AO		Guidance	
12	(i)	(a)	$R = mg\cos 30$	B1	3.3	Е	Resolving perpendicular to the plane	
			$T = \frac{1}{4}mg$	B 1	1.1	Е	Resolving vertically for <i>B</i>	
				M1	3.3	Е	Resolving parallel to the plane – three	
							terms – allow signs and sin/cos	
							confusion	
			$T + F - mg\sin 30 = 0$	A1	1.1	C		
			$F = \mu (mg \cos 30)$	M1	3.3	Е	Use of $F = \mu R$	
			$1 \qquad (mg\sqrt{3}) 1$	M1	2.1	Α	Deriving equation in μ (and <i>m</i> and <i>g</i>)	
			$\left \frac{1}{4}mg + \mu\right \left \frac{mg}{2}\right - \frac{1}{2}mg = 0 \implies \mu = \dots$				and attempt to solve for μ –	
							dependent on previous M marks and	
							second B mark	
			$u = \sqrt{3}$	A1	2.2a	Α		
			$\mu = \frac{1}{6}$					
				[7]				
12	(i)	(b)	$F = mg\sin 30 - \lambda mg(>0)$	M1	3.1a	Α	Resolving parallel to the plane with	
							λmg	
			$F > 0 \Longrightarrow \lambda < \frac{1}{2}$		2.2a	A		
			2	[2]				
12	(ii)		$T - F - mg\sin 30 = m\left(\frac{1}{4}g\right)$	M1	3.3	С	N, II parallel to the plane – four terms	Allow a
			$2mg - T = 2m\left(\frac{1}{4}g\right)$	B1	3.3	С	N, II for <i>B</i>	Allow <i>a</i>
			$2mg - F - mg\sin 30 = \frac{3}{4}mg$	A1	1.1	С	Correct method for eliminating <i>T</i>	
			$2ma$ $u(ma \cos 20)$ $ma \sin 20 - 3ma$	A1	2.1	А	Correct use of $F = \mu R$ and	
			$2mg - \mu(mg\cos 50) - mg\sin 50 = \frac{1}{4}mg$				$R = mg\cos 30$	
			5	Δ1	2.29	Δ		
			$\mu = \frac{\sqrt{3}}{2}$	[5]	2.2a	17		
			2	[-]				

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