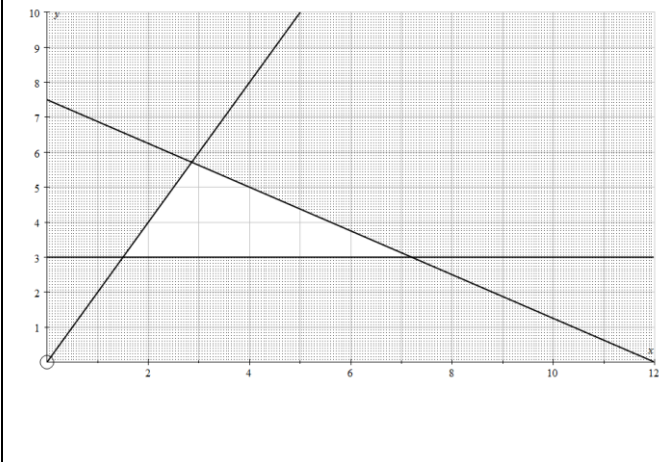
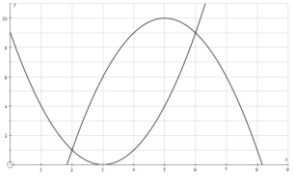


Question		Answer	Marks	Guidance	
9	(a)	$f(0) = -1, f(1) = 1$	M1	Substitution of both 0 and 1	
			A1	Both correct	
			[2]		
	(b)	$x^3 + 2x^2 - x - 1 = 0 \Rightarrow x^2(x+2) = (x+1)$ $\Rightarrow x^2 = \frac{(x+1)}{(x+2)} \Rightarrow x = \sqrt{\frac{(x+1)}{(x+2)}}$ AG	M1	Factorising the first two terms; x^2 must be seen as a factor	Alternatively: start from given eqn Square both sides and multiply up M1 Correct algebra seen to give original equation A1
A1			Ignore \pm		
			[2]		
	(c)	0.8 0.801784 0.801926 0.801937 x_3 $(\Rightarrow \gamma) = 0.802$	M1	Use of formula	Accept $\frac{3\sqrt{14}}{14}$ oe for x_1 Accept $x_3 = 0.802$ as final answer
A1			x_1 correct to at least 4 dp or exact		
			A1	At least x_3 correct to at least 4 dp seen and answer correct to 3sf	
			[3]		

Question		Answer	Marks	Guidance	
10	(a)	$x^2 + (2x+k)^2 = 5$ $\Rightarrow x^2 + 4x^2 + 4kx + k^2 - 5 = 0$ $\Rightarrow 5x^2 + 4kx + (k^2 - 5) = 0$ AG	M1 A1	Substitute and attempt to simplify	
			[2]		
	(b)	For coincident roots, the terms under the square root sign sum to 0 $\Rightarrow 16k^2 - 20(k^2 - 5) = 0$ $\Rightarrow -4k^2 + 100 = 0$ $\Rightarrow k = \pm 5$	M1 A1	Evidence of understanding that tangent implies coincident roots	“Evidence” means some indication that roots are coincident
			[2]		

Question		Answer	Marks	Guidance	
11	(a)	$5x+8y \leq 60$ oe	B1		
			[1]		
	(b)	$y \geq 3$	B1		
		$y \leq 2x$	B1		
			[2]		
	(c)		B3,2,1	<p>B1 for each line. Ignore errors in (a) and (b) Ignore labels for lines on graph</p> <p>B1 Correct shading</p>	<p>Check for time line goes through (4,5)</p> <p>Do not accept the shaded region being the triangle</p> <p>N.B. You might see lines on the graph that relate to (d) and (e) - ignore</p>
			[4]		
	(d)	$(x + y =) 10$ Time = 59 (hours)	B1 B1	$x = 7, y = 3$ only is B0	
			[2]		
	(e)	4 small and 5 large Profit = £412	M1 A1 A1	<p>Sight of $(P =) 28x + 60y$ on grid</p> <p>Or listing at least two correct feasible points and calculating P for each point</p> <p>soi by £412</p>	<p>SC no working seen but answer given, B1 B1</p> <p>Allow B2 by implication from £412</p>
			[3]		

Question		Answer	Marks	Guidance	
12	(a)	$10 = 10 \times 5 - 5^2 + k$ oe $\Rightarrow k = 10 - 25 = -15$ AG	M1 A1	Substitute	Either substitute (5, 10) to obtain k or substitute $k = -15$ and show that it is satisfied by (5, 10)
			[2]		
	(b)	$\frac{dy}{dx} = 10 - 2x$ $= 0$ when $x = 5$	M1 A1 A1	Diffn and set = 0 or find = 0 from $x = 5$ Any demonstration to show maximum	All powers reduced by 1 – beware of division by x e.g. gradient either side of turning points or values either side or $\frac{d^2y}{dx^2} = -2 < 0$ stated meaning maximum
		Alternative method: $y = a \pm (x \pm b)^2$ $= (10 - (x - 5)^2)$ \Rightarrow Maximum value of 10 when $x = 5$	M1 A1 A1	Completing the square	$a \neq -15$ and $b \neq 10$
		Alternative method: Statement that Quadratic function is symmetric Pair of symmetric coordinates either side of (5, 10) Gives maximum	M1 A1 A1		e.g. at $x = 4, 6, y = 9$ and $10 > 9$
			[3]		
	(c)		B1 B1	Upside down parabola Maximum (5, 10); Meets other curve at two points	
			[2]		

	(d)	(2, 1) and (6, 9)	B1 B1	FT <i>their</i> graphs FT <i>their</i> graphs	Accept an algebraic method that may differ from their intersections in (c)
			[2]		
	(e)	$\text{Area} = \int_2^6 (y_1 - y_2) dx$ $= \int_2^6 (16x - 2x^2 - 24) dx$ $= \left[8x^2 - \frac{2}{3}x^3 - 24x \right]_2^6$ $= (288 - 144 - 144) - \left(32 - \frac{16}{3} - 48 \right)$ $= 0 - \left(-\frac{64}{3} \right) = \pm \frac{64}{3}$ <p>Alternative method:</p> $\text{Area} = \int_2^6 y_1 dx - \int_2^6 y_2 dx$ $= \int_2^6 (10x - x^2 - 15) dx - \int_2^6 (x^2 - 6x + 9) dx$ $= \left[5x^2 - \frac{x^3}{3} - 15x \right]_2^6 - \left[\frac{x^3}{3} - 3x^2 + 9x \right]_2^6$ $= \left((180 - 72 - 90) - \left(20 - \frac{8}{3} - 30 \right) \right) - \left((72 - 108 + 54) - \left(\frac{8}{3} - 12 + 18 \right) \right)$ $= \left(18 + \frac{38}{3} \right) - \left(18 - \frac{26}{3} \right)$ $= \frac{92}{3} - \frac{28}{3} = \frac{64}{3}$	M1 A1 M1* M1* A1 M1 M1 A1 M1* A1	Difference of curves Or – this function Dep Integrate; ignore limits Dep Apply limits by substitution of <i>their</i> intersections, subtract in correct order Accept to 3sf or better Integrate both; ignore limits Apply limits in one integral by substitution of <i>their</i> intersections, subtract in correct order For one value Dep on both Subtract	In either order A0 if divided by 2 At least two powers increased by 1; beware multiplication by x SC answer with no working B5
			[5]		

Question		Answer	Marks	Guidance
13	(a)	$\frac{h}{300} = \tan 7 \Rightarrow h = 36.8\dots$	M1 A1	Use tan ratio Sine rule may be used
			[2]	
	(b)	$CB^2 = 400^2 + 300^2 - 2 \times 300 \times 400 \times \cos 60$ $= 130000$ $\Rightarrow CB = 360.55\dots$ elevation = $\tan^{-1}\left(\frac{\text{their } h}{\text{their } CB}\right)$ $= 5.83\dots$	M1 A1 A1 M1 A1	Find CB by correct cosine rule Correct substitutions Ignore any rounding Correct angle Correct to 3 sf
			[5]	
	(c)	e.g. $\frac{\sin B}{300} = \frac{\sin 60}{\text{their } CB}$ $\Rightarrow B = 46.1$ or $C = 73.9$ Bearing = $180 + 60 + \text{their } B$ $= 286^\circ$	M1 A1 A1 M1 A1	Either sin rule or cosine rule to find angle at B or C Alternative methods ok Inserting correct values into chosen formula correctly awrt 46 or 74 Correct attempt to find bearing awrt 286 rearranging correctly either sin = or cos = Or using C
			[5]	

Question		Answer	Marks	Guidance
14	(a)	$\frac{dv}{dt} = a \text{ (constant)} \Rightarrow v = c + at \Rightarrow v = 14 + at$ $\frac{ds}{dt} = v = 14 + at \Rightarrow s = c + 14t + \frac{1}{2}at^2 = 14t + \frac{1}{2}at^2$ $\Rightarrow 50 = 14t + \frac{1}{2}at^2 \text{ and } 9 = 14 + at \Rightarrow at = -5$ $\Rightarrow 50 = 14t - \frac{5}{2}t = \frac{23}{2}t \Rightarrow t = \frac{100}{23} \approx 4.35$ $\Rightarrow a = -\frac{23}{20} = -1.15$	<p>M1</p> <p>A1</p> <p>A1</p>	
		<p>Alternative method: $u = 14, v = 9, s = 50$ Use of $v^2 = u^2 + 2as \Rightarrow 100a = 9^2 - 14^2$ $\Rightarrow a = -1.15$ Use of $v = u + at \Rightarrow t = \frac{5}{1.15} = 4.35$</p>	<p>M1</p> <p>A1</p> <p>A1</p>	<p>Use of at least one correct suvat formulae to get a or t www</p> <p>www</p>
		<p>Alternative method: $s = (\text{Average velocity}) \times \text{time}$ $\Rightarrow 50 = \frac{9+14}{2}t \Rightarrow t = \frac{100}{23} = 4.35$ $\Rightarrow a = \frac{9-14}{4.35} = -1.15$</p>	<p>M1</p> <p>A1</p> <p>A1</p>	<p>Allow 1.15 if it is clear that a is the deceleration</p> <p>Correct suvat formula is $v^2 = u^2 + 2as, v = u + at, s = \frac{(u+v)}{2}t$</p>
			[3]	

	(b)	$v = 14$	B1	Substitute $t = 10$	Or substitute $v = 14$ to give cubic in t and $t = 10$ shown to be a root The cubic is $t^3 - 15t^2 + 500 = 0$
			[1]		
	(c)	$v = \frac{1}{100}(15t^2 - t^3) + 9$ $\Rightarrow s = \frac{1}{100}\left(5t^3 - \frac{t^4}{4}\right) + 9t$ $\Rightarrow s = \frac{1}{100}(5000 - 2500) + 90$ $= 115$	M1 A1 M1* A1	Integrate - at least two powers increased by 1. Beware multiplying by t Ignore c Dep Substitute $t = 10$	M0 if 1/100 integrated Beware: suvat formulae will give 115
			[4]		
	(d)	$v = \frac{1}{100}(15t^2 - t^3) + 9$ $\Rightarrow a = \frac{1}{100}(30t - 3t^2)$ $\Rightarrow \frac{da}{dt} = \frac{1}{100}(30 - 6t) = 0 \text{ when } t = 5$ $\Rightarrow a = \frac{1}{100}(150 - 75) = 0.75$ <p>Alternative method: Differentiate once and use symmetry of quadratic or complete square Correct diffn and completed square or symmetry around 5 $a = 0.75$</p>	M1 A1 A1 M1 A1 A1	Differentiate twice Symmetry must be stated	
			[3]		
	(e)	Distance between bumps = <i>their</i> $115 + 50 = 165$ m	B1	FT their answer to (c)	
			[1]		

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