GENERAL CERTIFICATE OF SECONDARY EDUCATION

MATHEMATICS A

Unit B (Higher Tier)

INSTRUCTIONS TO CANDIDATES

• Write your name, centre number and candidate number in the boxes above. Please write clearly and in capital letters.
• Use black ink. Pencil may be used for graphs and diagrams only.
• Read each question carefully. Make sure you know what you have to do before starting your answer.
• Your answers should be supported with appropriate working. Marks may be given for a correct method even if the answer is incorrect.
• Write your answer to each question in the space provided. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
• Answer all the questions.
• Do not write in the bar codes.

INFORMATION FOR CANDIDATES

• The number of marks is given in brackets [ ] at the end of each question or part question.
• Your Quality of Written Communication is assessed in questions marked with an asterisk (*).
• The total number of marks for this paper is 60.
• This document consists of 16 pages. Any blank pages are indicated.

WARNING
No calculator can be used for this paper

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This paper has been pre modified for carrier language

Turn over
Area of trapezium = \( \frac{1}{2} (a + b)h \)

Volume of prism = (area of cross-section) \times \text{length}

In any triangle \( \triangle ABC \)

Sine rule \( \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \)

Cosine rule \( a^2 = b^2 + c^2 - 2bc \cos A \)

Area of triangle = \( \frac{1}{2} ab \sin C \)

Volume of sphere = \( \frac{4}{3} \pi r^3 \)

Surface area of sphere = \( 4\pi r^2 \)

Volume of cone = \( \frac{1}{3} \pi r^2 h \)

Curved surface area of cone = \( \pi rl \)

The Quadratic Equation
The solutions of \( ax^2 + bx + c = 0 \), where \( a \neq 0 \), are given by
\[
x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}
\]
1  (a) Work out.
    (i) the cube of 5

    (a)(i) ___________________________ [1]

    (ii) \( \sqrt{169} \)

    (ii) ___________________________ [1]

(b) (i) Write as a single power of 5.
      \( 5^6 \times 5^4 \)

    (b)(i) ___________________________ [1]

    (ii) Write as a single power of \( r \).
      \( \frac{r^{12}}{r^3} \)

    (ii) ___________________________ [1]

(c) Find the value of the following.
    (i) \( 16^0 \)

    (c)(i) ___________________________ [1]

    (ii) \( 27^{\frac{2}{3}} \)

    (ii) ___________________________ [2]
(a) Rotate shape \( F \) 90° anticlockwise about the point (1, 1).
Label the image \( G \). [3]

(b) Translate shape \( F \) using the vector \( \begin{pmatrix} 1 \\ -3 \end{pmatrix} \).
Label the image \( H \). [2]
A DIY store sells nails in boxes, which are cuboids.

Each full box of nails weighs 250 g.
The boxes are delivered in crates which are cubes of side 0.4 m.
An empty crate weighs 20 kg.

How much, in kg, would a crate full of these boxes of nails weigh?

__________________________ kg [4]
4  (a) Solve this inequality.

\[ 3x - 2 \leq 10 \]

(b) Represent your solution to part (a) on this number line.

\[ \begin{array}{cccccccc}
-2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\
\end{array} \]
Petra is designing a small mat to put a glass on. She decides to make the mat a **regular** hexagon. All the corners should lie on the circle, centre O. One of the corners should be at point A.

Construct the hexagon.
Sam bought an electronic game on Monday 11th October. The game gives him word and number puzzles to test how well his brain works. He can practise the puzzles to try to improve. The game gives him a ‘Brain Age’ to show how well he is doing.

The Brain Age can range from 65, which is very poor, to 20, which is best.

The game uses a time series graph to show Sam’s Brain Age.

(a) Complete the time series graph with this information.

<table>
<thead>
<tr>
<th>Date</th>
<th>Sam’s Brain Age</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fri 5 Nov</td>
<td>34</td>
</tr>
<tr>
<td>Sat 6 Nov</td>
<td>34</td>
</tr>
<tr>
<td>Sun 7 Nov</td>
<td>33</td>
</tr>
<tr>
<td>Mon 8 Nov</td>
<td>31</td>
</tr>
<tr>
<td>Tues 9 Nov</td>
<td>30</td>
</tr>
<tr>
<td>Wed 10 Nov</td>
<td>30</td>
</tr>
<tr>
<td>Thur 11 Nov</td>
<td>28</td>
</tr>
</tbody>
</table>
(b) One day Sam discovers a method to get much better scores.

On what date did Sam discover this method?

(b) ______________________ [1]

(c) Sam realises he does not do as well when he is ill.
Sam was ill for two days in October.

On which dates was he ill?

(c) ______________________ [1]

(d) Sam’s father, John, also likes to play the game occasionally.

<table>
<thead>
<tr>
<th>Date</th>
<th>John’s Brain Age</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tues 12 Oct</td>
<td>38</td>
</tr>
<tr>
<td>Wed 20 Oct</td>
<td>30</td>
</tr>
<tr>
<td>Sat 23 Oct</td>
<td>35</td>
</tr>
<tr>
<td>Mon 1 Nov</td>
<td>28</td>
</tr>
<tr>
<td>Thur 11 Nov</td>
<td>29</td>
</tr>
</tbody>
</table>

(i) On the grid, draw the time series graph for John’s Brain Age. [1]

(ii) Sam thinks he will soon be able to get a better Brain Age than his father all the time.

Is Sam correct?
Explain your answer.

_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________

_____________________________________________________________________

[2]
7  (a) The sketches of three different straight line graphs are shown below.

Write the correct equation under each sketch. Choose from this list.

\[ y = \frac{1}{2}x + 5 \quad y = -3x + 5 \quad y = x^2 + 5 \quad y = x - 5 \quad y = -3x - 5 \]

(b) A line, \( L \), is perpendicular to the line \( y = 2x + 6 \). 
\( L \) goes through the point \( (0, 3) \).

Find the equation of the line \( L \).
This scatter graph shows the time taken to run 100 metres plotted against age for a group of 18 people.

Lizzie says that, for these people, there is **no correlation** between age and time taken to run 100m.

Parand says that, for these people, there is **a relationship** between age and time taken to run 100m.

Is Lizzie correct? Is Parand correct?

Explain your conclusions clearly.

_____________________________________________________________________________
_____________________________________________________________________________
_____________________________________________________________________________
_____________________________________________________________________________
_____________________________________________________________________________
_____________________________________________________________________________
[4]
The Park and Ride is a bus service to take people into the city centre. Adults pay £1.60 for a ticket and children pay 20 pence. On one journey there are 55 passengers and the driver collects £67.

Let \( a \) be the number of adults on the bus and let \( c \) be the number of children on the bus.

(a) Show that \( 8a + c = 335 \).

(b) The fact that there are 55 passengers means that \( a + c = 55 \).

Solve this equation simultaneously with the one from part (a) to find how many children are on the bus.
10  The three-toed sloth is a very slow-moving animal. In 2 \( \frac{3}{4} \) hours it can only travel \( \frac{33}{80} \) of a mile.

Use the formula

\[
\text{speed} = \frac{\text{distance}}{\text{time}}
\]

to calculate its average speed in miles per hour. Give your answer as a fraction in its simplest form.

\[
\text{_______________ mph [3]}
\]
11 A, B, C and D are points on a circle.

(a) Work out angle $p$. Give a reason for your answer.

$p = \underline{\phantom{0}}^\circ$ because __________________________________________________________

______________________________________________________________________ [2]

(b)* Is the diameter of the circle less than 8 cm, more than 8 cm or equal to 8 cm? Justify your answer.

________________________________________________________________________

________________________________________________________________________

________________________________________________________________________ [3]
12 Write the following in the form $a\sqrt{3}$, where $a$ is an integer.

(a) $\frac{6}{\sqrt{3}}$

(a) ______________________ [2]

(b) $\sqrt{24} \times \sqrt{2}$

(b) ______________________ [2]

TURN OVER FOR QUESTION 13
13 (a) On the grid, draw the line $3x + 4y = 12$.

(b) On the grid, indicate clearly the region $R$ which satisfies all the following inequalities.

$3x + 4y < 12$
$x > 1$
$y > 0$

(c) Write down the integer values of $x$ and $y$ that satisfy all three inequalities.

(c) $x = \quad \quad \quad y = \quad \quad \quad$ [1]